

MATHEMATICS STANDARD ARTICULATED BY GRADE LEVEL

Kindergarten

Instruction for students identified as having a significant cognitive disability should be developed from Arizona's Alternate Academic Standards. Only those performance objectives that have an identified alternate are required. When developing lessons or activities aligned to the grade level alternate standards, teachers should consider individual student abilities and their need for accommodations, cues, manipulatives/objects, augmentative devices, and communication systems. In addition the depth and breadth of the alternate academic standard can be simplified based on the student's current cognitive abilities. Teachers can also develop lessons using performance objectives without alternates for those students who have developed those specific skills.

Strand 1: Number Sense and Operations

Concept 1: Number Sense	
Understand and apply numbers, ways of representing numbers, the relationships among numbers and different number systems.	
PO 1.	Make a model to represent a given whole number 0 through 20. Alternate: Identify models of whole numbers 0 through 5.
PO 2.	Identify orally a whole number represented by a model with a word name and symbol 0 through 20. (Say 3 and write number 3 when presented with three objects.) Alternate: Identify words with symbols to represent whole numbers 0 through 5.
PO 3.	Count aloud, forward to 20 or backward from 10, in consecutive order (0 through 20).
PO 4.	Identify whole numbers through 20 in or out of order. Alternate: Identify whole numbers through 5, in or out of order.
PO 5.	Write whole numbers through 20 in or out of order. Alternate: Write whole numbers 0 through 5, in or out of order.
PO 6.	Construct equivalent forms of whole numbers, using manipulatives, through 10 (e.g., $\square\square + \square\square = \square\square\square + \square$).
PO 7.	Compare two whole numbers through 20.
PO 8.	Recognize the ordinal numbers through fifth (e.g., first, second, third). Alternate: Recognize ordinal positions first and last.
PO 9.	Order three or more whole numbers through 20 (least to greatest or greatest to least).
PO 10.	Identify penny, nickel, dime, quarter, and dollar by using manipulatives or pictures. Alternate: Identify coins or bills as money.

Concept 2: Numerical Operations

Understand and apply numerical operations and their relationship to one another.

- PO 1. Model addition through sums of 10 using manipulatives.
- PO 2. Model subtraction with minuends of 10 using manipulatives.
- PO 3. Select the operation to solve word problems using numbers 0 through 9.
- PO 4. Solve word problems presented orally using addition or subtraction with numbers through 9.
- PO 5. Identify the symbols: +, -, =.
Alternate: Identify the symbols +, -, or =.
- PO 6. Use grade-level appropriate mathematical terminology.

Concept 3: Estimation

Use estimation strategies reasonably and fluently.

- PO 1. Solve problems using a variety of mental computations and reasonable estimations.

Strand 2: Data Analysis, Probability, and Discrete Mathematics

Concept 1: Data Analysis (Statistics)

Understand and apply data collection, organization and representation to analyze and sort data.

- PO 1. Formulate questions to collect data in contextual situations.
- PO 2. Interpret a pictograph.
Alternate: Identify a pictograph.
- PO 3. Answer questions about a pictograph.
- PO 4. Formulate questions based on data displayed in graphs, charts, and tables.
- PO 5. Solve problems based on simple graphs, charts, and tables.
Alternate: Answer questions based on simple pictographs.

Concept 2: Probability

Understand and apply the basic concepts of probability.

(Grades 2-HS)

Concept 3: Discrete Mathematics – Systematic Listing and Counting

Understand and demonstrate the systematic listing and counting of possible outcomes.

- PO 1. Make arrangements that represent the number of combinations that can be formed by pairing items taken from 2 sets, using manipulatives (e.g., How many outfits can one make with 2 different color shirts and 2 different pairs of pants?).

Concept 4: Vertex-Edge Graphs

Understand and apply vertex-edge graphs.

- PO 1. Color pictures with the least number of colors so that no common edges share the same color (increased complexity throughout grade levels).

Strand 3: Patterns, Algebra, and Functions

Concept 1: Patterns

Identify patterns and apply pattern recognition to reason mathematically.

PO 1. Communicate orally a grade-level appropriate pattern.

PO 2. Extend simple repetitive patterns using manipulatives.
Alternate: Identify patterns.

PO 3. Create grade-level appropriate patterns.

Concept 2: Functions and Relationships

Describe and model functions and their relationships.

(Grades 2-HS)

Concept 3: Algebraic Representations

Represent and analyze mathematical situations and structures using algebraic representations.

(Grades 1-HS)

Concept 4: Analysis of Change

Analyze change in a variable over time and in various contexts.

(Grades 1-HS)

Strand 4: Geometry and Measurement

Concept 1: Geometric Properties

Analyze the attributes and properties of 2- and 3- dimensional shapes and develop mathematical arguments about their relationships.

PO 1. Identify 2-dimensional shapes by attribute (size, shape, number of sides).

PO 2. Identify concepts and terms of position and size in contextual situations:

- Inside/outside,
- Above/below/between,
- Smaller/larger, and
- Longer/shorter.

Alternate: Identify concepts and terms of position and size in contextual situations:

- **Inside/Outside**
- **Above/Below**
- **Smaller/Larger**

PO 3. Identify shapes in different environments (e.g., nature, buildings, classroom).

Concept 2: Transformation of Shapes

Apply spatial reasoning to create transformations and use symmetry to analyze mathematical situations.

(Grades 1-HS)

Concept 3: Coordinate Geometry

Specify and describe spatial relationships using coordinate geometry and other representational systems.

(Grades 3-HS)

Concept 4: Measurement - Units of Measure - Geometric Objects

Understand and apply appropriate units of measure, measurement techniques, and formulas to determine measurements.

PO 1. Verbally compare objects according to observable and measurable attributes.

PO 2. Communicate orally how different attributes of an object can be measured.

PO 3. Order objects according to observable and measurable attributes.

Strand 5: Structure and Logic

Concept 1: Algorithms and Algorithmic Thinking

Use reasoning to solve mathematical problems in contextual situations.

(Grades 1-HS)

Concept 2: Logic, Reasoning, Arguments, and Mathematical Proof

Evaluate situations, select problem-solving strategies, draw logical conclusions, develop and describe solutions and recognize their applications.

PO 1. Sort objects according to observable attributes.

Alternate: Sort objects according to one observable attribute.

PO 2. Provide rationale for classifying objects according to observable attributes (color, size, shape, weight, etc.).

MATHEMATICS STANDARD ARTICULATED BY GRADE LEVEL

Grade 1

Instruction for students identified as having a significant cognitive disability should be developed from Arizona's Alternate Academic Standards. Only those performance objectives that have an identified alternate are required. When developing lessons or activities aligned to the grade level alternate standards, teachers should consider individual student abilities and their need for accommodations, cues, manipulatives/objects, augmentative devices, and communication systems. In addition the depth and breadth of the alternate academic standard can be simplified based on the student's current cognitive abilities. Teachers can also develop lessons using performance objectives without alternates for those students who have developed those specific skills.

Strand 1: Number Sense and Operations

Concept 1: Number Sense	
Understand and apply numbers, ways of representing numbers, the relationships among numbers and different number systems.	
PO 1.	Make a model to represent a given whole number 0 through 100. Alternate: Identify models to represent whole numbers 0 through 10.
PO 2.	Identify a whole number represented by a model with a word name and symbol 0 through 100. Alternate: Identify models with a word symbol to represent whole numbers 0 through 10.
PO 3.	Count aloud, forward or backward, in consecutive order (0 through 100). Alternate: Count forward through 10.
PO 4.	Identify whole numbers through 100 in or out of order. Alternate: Identify whole numbers through 10, in or out of order.
PO 5.	Write whole numbers through 100 in or out of order. Alternate: Write whole numbers 0 through 10, in or out of order.
PO 6.	Construct equivalent forms of whole numbers, using manipulatives or symbols, through 99 (e.g., $15 + 5 = 10 + 10$).
PO 7.	State verbally whole numbers, through 100, using correct place value (e.g., A student will read 84 as eight tens and four ones.).
PO 8.	Construct models to represent place value concepts for the one's and ten's places.
PO 9.	Apply expanded notation to model place value through 99 (e.g., $37 = 3$ groups of ten + 7 units).
PO 10.	Identify odd and even whole numbers through 100.
PO 11.	Compare two whole numbers through 100.
PO 12.	Use ordinal numbers through tenth. Alternate: Recognize ordinal positions first, second, and third.
PO 13.	Order three or more whole numbers through 100 (least to greatest or greatest to least).

- PO 14. Make models that represent given fractions (halves).
- PO 15. Identify in symbols and in words a model that is divided into equal fractional parts (halves).
- PO 16. Identify money by name and value: penny, nickel, dime, quarter, and one dollar.
Alternate: Identify penny and dollar by name.
- PO 17. Count money through \$1.00 using coins.
- PO 18. Identify the value of a collection of coins using the symbols ¢ and \$.

Concept 2: Numerical Operations

Understand and apply numerical operations and their relationship to one another.

- PO 1. Demonstrate the process of addition through sums of 20 using manipulatives.
Alternate: Demonstrate the process of addition.
- PO 2. Demonstrate the process of subtraction with minuends of 20 using manipulatives.
- PO 3. State addition facts for sums through 18 and subtraction for differences with minuends through 9 or less.
- PO 4. Add one- and two-digit whole numbers without regrouping.
- PO 5. Subtract one- and two-digit whole numbers without regrouping.
- PO 6. Select the grade-level appropriate operation to solve word problems.
- PO 7. Solve word problems using addition and subtraction of 2-digit numbers without regrouping.
- PO 8. Count by multiples to show the process of multiplication (10s, 5s, or 2s).
- PO 9. Demonstrate families of equations for addition and subtraction through 18.
- PO 10. Demonstrate the identity and commutative properties of addition through 18.
- PO 11. Identify addition and subtraction as inverse operations.
- PO 12. Apply the symbols: +, -, =.
Alternate: Use the symbols + and = .
- PO 13. *Use grade-level appropriate mathematical terminology.*
- PO 14. Demonstrate addition of fractions with like denominators (halves) using models.
- PO 15. Demonstrate subtraction of fractions with like denominators (halves) using models.
- PO 16. Add and subtract money without regrouping using manipulatives and paper and pencil, through 99¢.

Concept 3: Estimation

Use estimation strategies reasonably and fluently.

PO 1. *Solve problems using a variety of mental computations and reasonable estimation.*

PO 2. Estimate the measurement of an object using U.S. customary standard and non-standard units of measurement.

Alternate: Estimate the measurement of an object by comparing it to another as being larger or smaller.

Strand 2: Data Analysis, Probability, and Discrete Mathematics

Concept 1: Data Analysis (Statistics)

Understand and apply data collection, organization and representation to analyze and sort data.

- PO 1. *Formulate questions to collect data in contextual situations.*
- PO 2. Make a simple pictograph or tally chart with appropriate labels from organized data.
Alternate: Match a pictograph to labels.
- PO 3. Interpret pictographs using terms such as most, least, equal, more than, less than, and greatest.
- PO 4. Answer questions about pictographs using terms such as most, least, equal, more than, less than, and greatest.
- PO 5. *Formulate questions based on graphs, charts, and tables.*
- PO 6. *Solve problems using graphs, charts, and tables.*
Alternate: Answer questions based on simple graphs.

Concept 2: Probability

Understand and apply the basic concepts of probability.

(Grades 2-HS)

Concept 3: Discrete Mathematics – Systematic Listing and Counting

Understand and demonstrate the systematic listing and counting of possible outcomes.

- PO 1. *Make arrangements that represent the number of combinations that can be formed by pairing items taken from 2 sets, using manipulatives (e.g., How many ice cream cones can one make with 2 different types of ice cream and 2 different types of cones?).*

Concept 4: Vertex-Edge Graphs

Understand and apply vertex-edge graphs.

- PO 1. *Color pictures with the least number of colors so that no common edges share the same color (increased complexity throughout grade levels).*

Strand 3: Patterns, Algebra, and Functions

Concept 1: Patterns

Identify patterns and apply pattern recognition to reason mathematically.

- PO 1. *Communicate a grade-level appropriate pattern* (e.g., ♦, ▽, ♥ Repeat this complete pattern.)
- PO 2. Extend a simple grade-level appropriate repetitive pattern (e.g., ↑, ↓, ↑, ↓, ↑, ____, ____,)
Alternate: Extend a pattern of symbols or pictures.
- PO 3. *Create grade-level appropriate patterns.*

Concept 2: Functions and Relationships

Describe and model functions and their relationships.

(Grades 2-HS)

Concept 3: Algebraic Representations

Represent and analyze mathematical situations and structures using algebraic representations.

- PO 1. Use variables in contextual situations.
- PO 2. *Find the missing sum or difference in number sentences for sums and minuends through 9 (e.g., $2 + 5 = _$).

Concept 4: Analysis of Change

Analyze change in a variable over time and in various contexts.

- PO 1. Identify the change in a variable over time (e.g., an object gets taller, colder, heavier,
- PO 2. Make simple predictions based on a variable (e.g., select next stage of plant growth).

Strand 4: Geometry and Measurement

Concept 1: Geometric Properties

Analyze the attributes and properties of 2- and 3- dimensional shapes and develop mathematical arguments about their relationships.

PO 1. Use the words vertex and side when describing simple 2-dimensional geometric shapes.

PO 2. *Identify 2-dimensional shapes by attribute* (size, shape, number of sides, vertices).

PO 3. Use concepts and terms of position and size in contextual situations:

- Inside/outside,
- Left/right,
- Above/below/between,
- Smaller/larger, and
- Longer/shorter.

Alternate: Identify concepts and terms of position and size in contextual situations:

- *Inside/Outside,*
- *Above/Below,*
- *Smaller/larger*

PO 4. Name common 2-dimensional shapes (square, rectangle, triangle, circle).

Alternate: Identify common shapes in context (square, circle, and triangle).

PO 5. Draw 2-dimensional shapes (square, rectangle, triangle, circle).

PO 6. Recognize where a line of symmetry divides a 2-dimensional shape into mirror images.

Concept 2: Transformation of Shapes

Apply spatial reasoning to create transformations and use symmetry to analyze mathematical situations.

PO 1. Recognize same shape in different positions (slide/translations).

Concept 3: Coordinate Geometry

Specify and describe spatial relationships using coordinate geometry and other representational systems.

(Grades 3-HS)

**Concept 4: Measurement - Units of Measure
- Geometric Objects**

Understand and apply appropriate units of measure, measurement techniques, and formulas to determine measurements.

- PO 1. Compare the measurable characteristics of two objects (e.g., length, weight, size).
Alternate: Compare the measurable characteristics of two objects (bigger/smaller).
- PO 2. Select the appropriate measure of accuracy:
- length – inches, feet,
 - capacity/volume – cups, gallons, and
 - mass/weight – pounds.
- PO 3. Tell time to the hour using analog and digital clocks.
Alternate: Identify that time can be read on a clock.
- PO 4. Name the days of the week for yesterday, today, and tomorrow (e.g., If today is Wednesday, what day will it be tomorrow?).
Alternate: Identify that days of the week can be found on a calendar.
- PO 5. Name the 12 months of the year in proper order, starting with January.
- PO 6. Name the 7 days of the week in proper order, starting with Sunday.
- PO 7. Measure a given object using the appropriate unit of measure:
- length – inches, feet and yards,
 - capacity/volume – cups, gallons, and
 - mass/weight – pounds.
- Alternate: Identify that objects can be measured.**

Strand 5: Structure and Logic

Concept 1: Algorithms and Algorithmic Thinking

Use reasoning to solve mathematical problems in contextual situations.

PO 1. Create problems based on contextual situations (addition facts up to 18 and subtraction from 9).

Concept 2: Logic, Reasoning, Arguments, and Mathematical Proof

Evaluate situations, select problem-solving strategies, draw logical conclusions, develop and describe solutions and recognize their applications.

PO 1. List the quantitative components found in word problems.

PO 2. *Provide rationale for classifying objects according to observable attributes (color, size, shape, weight, etc.).*

Alternate: Sort objects by length.

MATHEMATICS STANDARD ARTICULATED BY GRADE LEVEL

Grade 2

Instruction for students identified as having a significant cognitive disability should be developed from Arizona's Alternate Academic Standards. Only those performance objectives that have an identified alternate are required. When developing lessons or activities aligned to the grade level alternate standards, teachers should consider individual student abilities and their need for accommodations, cues, manipulatives/objects, augmentative devices, and communication systems. In addition the depth and breadth of the alternate academic standard can be simplified based on the student's current cognitive abilities. Teachers can also develop lessons using performance objectives without alternates for those students who have developed those specific skills.

Strand 1: Number Sense and Operations

Concept 1: Number Sense

Understand and apply numbers, ways of representing numbers, the relationships among numbers and different number systems.

- PO 1. Make a model to represent a given whole number 0 through 999.
Alternate: Identify models to represent whole numbers 0 through 15.
- PO 2. Identify a whole number represented by a model with a word name and symbol 0 through 999.
Alternate: Identify models with a word symbol to represent whole numbers 0 through 15.
- PO 3. Count aloud, forward or backward, in consecutive order (0 through 999).
Alternate: Count forward through 15.
- PO 4. Identify whole numbers through 999 in or out of order.
Alternate: Identify whole numbers through 15, in or out of order.
- PO 5. Write whole numbers through 999 in or out of order.
Alternate: Write whole numbers 0 through 15, in or out of order.
- PO 6. State equivalent forms of whole numbers using multiples of 10 through 1,000 ($430 + 200 = 600 + 30$).
- PO 7. State verbally whole numbers, through 999, using correct place value (e.g., A student will read 528 as five hundreds, two tens, and eight ones.).
- PO 8. Construct models to represent place value concepts for the one's, ten's, and hundred's places.
- PO 9. Apply expanded notation to model place value through 999 (e.g., $378 = 3 \text{ hundreds} + 7 \text{ tens} + 8 \text{ ones}$).
- PO 10. Identify odd and even (including 0) whole numbers through 999.

- PO 11. Compare two whole numbers through 999.
- PO 12. Use ordinal numbers.
Alternate: Use ordinal positions first, second, and third.
- PO 13. Order three or more whole numbers through 999 (least to greatest or greatest to least).
- PO 14. Make models that represent given fractions (halves and fourths).
- PO 15. Identify in symbols and words a model that is divided into equal fractional parts (halves and fourths).
Alternate: Identify a model as whole or half.
- PO 16. Count money through \$5.00 using manipulatives and pictures of bills and coins.
- PO 17. Identify the value of a collection of money using the symbols ¢ and \$ through \$5.00.
Alternate: Identify penny, nickel, dime, and dollar by name.
- PO 18. Use decimals through hundredths in contextual situations with money.
- PO 19. Compare two decimals using money, through hundredths, using models, illustrations, or symbols.
- PO 20. Distinguish the equivalency among decimals, fractions and percents (e.g., half-dollar = 50¢ = 50%).

Concept 2: Numerical Operations

Understand and apply numerical operations and their relationship to one another.

- PO 1. Demonstrate the process of addition through two three-digit whole numbers, using manipulatives.
Alternate: Demonstrate the process of addition through 10.
- PO 2. Demonstrate the process of subtraction using manipulatives with two-digit whole numbers.
Alternate: Demonstrate the process of subtraction.
- PO 3. State addition and subtraction facts.
- PO 4. Add one- and two-digit whole numbers with regrouping.
- PO 5. Subtract one- and two-digit whole numbers with regrouping.
- PO 6. Add 3 one- or two-digit addends.
- PO 7. *Select the grade-level appropriate operation to solve word problems.*
- PO 8. Solve word problems using addition and subtraction of two 2-digit numbers, with regrouping AND two 3-digit numbers without regrouping.
- PO 9. Count by multiples of three.
Alternate: Count by multiples of two.

- PO 10. State multiplication facts: 2s, 5s and 10s.
- PO 11. Demonstrate the associative property of addition [e.g., $(3 + 5) + 4 = 3 + (5 + 4)$].
- PO 12. *Apply grade-level appropriate properties to assist in computation.*
- PO 13. Apply the symbols: +, -, \times , \div , =, \neq , <, >, %.
Alternate: Use the symbols + and =.
- PO 14. *Use grade-level appropriate mathematical terminology.*
- PO 15. Demonstrate addition of fractions with like denominators (halves and fourths) using models.
- PO 16. Demonstrate subtraction of fractions with like denominators (halves and fourths) using models.
- PO 17. Add and subtract money without regrouping using manipulatives and paper and pencil, through \$5.00.

Concept 3: Estimation

Use estimation strategies reasonably and fluently.

- PO 1. *Solve problems using a variety of mental computations and reasonable estimation.*
Alternate: Estimate in a contextual situation.
- PO 2. *Estimate the measurement of an object using U.S. customary standard and non-standard units of measurement.*
- PO 3. Compare an estimate to the actual measure.
- PO 4. Evaluate the reasonableness of an estimate.

Strand 2: Data Analysis, Probability, and Discrete Mathematics

Concept 1: Data Analysis (Statistics)

Understand and apply data collection, organization and representation to analyze and sort data.

- PO 1. *Formulate questions to collect data in contextual situations.*
- PO 2. *Make a simple pictograph or tally chart with appropriate labels from organized data.*
Alternate: Match a simple pictograph to organized data.
- PO 3. *Interpret pictographs using terms such as most, least, equal, more than, less than, and greatest.*
- PO 4. *Answer questions about a pictograph using terms such as most, least, equal, more than, less than, and greatest.*
- PO 5. *Formulate questions based on graphs, charts, and tables.*
- PO 6. *Solve problems using graphs, charts, and tables.*
Alternate: Answer questions based on simple graphs.

Concept 2: Probability

Understand and apply the basic concepts of probability.

- PO 1. Name the possible outcomes for a probability experiment.
- PO 2. Predict the most likely or least likely outcome in probability experiments (e.g., Predict the chance of spinning one of the 2 colors on a 2-colored spinner.).
- PO 3. Predict the outcome of a grade-level appropriate probability experiment.
- PO 4. Record the data from performing a grade-level appropriate probability experiment.
- PO 5. Compare the outcome of an experiment to predictions made prior to performing the experiment.
- PO 6. Compare the results of two repetitions of the same grade-level appropriate probability experiment.

Concept 3: Discrete Mathematics – Systematic Listing and Counting

Understand and demonstrate the systematic listing and counting of possible outcomes.

- PO 1. *Make arrangements that represent the number of combinations that can be formed by pairing items taken from 2 sets, using manipulatives (e.g., How many types of sandwiches can one make with 3 different types of fillings and 2 types of bread if only one type of bread and 1 kind of filling is used for each sandwich?).*

Concept 4: Vertex-Edge Graphs

Understand and apply vertex-edge graphs.

- PO 1. *Color pictures with the least number of colors so that no common edges share the same color (increased complexity throughout grade levels).*

Strand 3: Patterns, Algebra, and Functions

Concept 1: Patterns

Identify patterns and apply pattern recognition to reason mathematically.

- PO 1. Communicate a grade-level appropriate pattern, using symbols or numbers (e.g., ∇ , O, Δ , ∇ , O, Δ , ∇ , ____, ____, ____).
- PO 2. *Extend a grade-level appropriate repetitive pattern* (e.g., 12, 22, 32, ____, ____, ____).
Alternate: Extend a pattern of symbols.
- PO 3. *Create grade-level appropriate patterns.*

Concept 2: Functions and Relationships

Describe and model functions and their relationships.

- PO 1. Describe the rule used in a simple grade-level appropriate function (e.g., T-chart, input/output model, and frames and arrows).

Concept 3: Algebraic Representations

Represent and analyze mathematical situations and structures using algebraic representations.

- PO 1. *Use variables in contextual situations.*
- PO 2. *Find the missing element (addend, subtrahend, minuend, sum, and difference) in addition and subtraction number sentences for sums through 18 and minuends through 9 (e.g., $13 - _ = 8$).

Concept 4: Analysis of Change

Analyze change in a variable over time and in various contexts.

- PO 1. *Identify the change in a variable over time* (e.g., *an object gets taller, colder, heavier*).
- PO 2. *Make simple predictions based on a variable* (e.g., *a child's height from year to year*).

Strand 4: Geometry and Measurement

Concept 1: Geometric Properties

Analyze the attributes and properties of 2- and 3- dimensional shapes and develop mathematical arguments about their relationships.

- PO 1. Compare attributes of 2-dimensional shapes (square, rectangle, triangle, and circle).
Alternate: Match simple shapes to names (square, circle, and triangle).
- PO 2. Recognize congruent shapes.
- PO 3. Recognize line(s) of symmetry for a 2-dimensional shape.

Concept 2: Transformation of Shapes

Apply spatial reasoning to create transformations and use symmetry to analyze mathematical situations.

- PO 1. *Recognize same shape in different positions (flip/reflection).*

Concept 3: Coordinate Geometry

Specify and describe spatial relationships using coordinate geometry and other representational systems.

(Grades 3-HS)

Concept 4: Measurement - Units of Measure - Geometric Objects

Understand and apply appropriate units of measure, measurement techniques, and formulas to determine measurements.

- PO 1. Identify the type of measure (e.g., weight, height, and time) for each attribute of an object.
- PO 2. Select the appropriate U.S. customary measure of accuracy:
- length – inches, feet, yards, miles,
 - capacity/volume – pints, quarts, and
 - mass/weight – ounces.
- Alternate: Demonstrate units of measure appropriate for a situation (inches and feet).**
- PO 3. Tell time to the quarter hour using analog and digital clocks.
Alternate: Match time to parts of the day.
- PO 4. Determine the passage of time using units of days and weeks within a month using a calendar.
- PO 5. Select the appropriate tool to measure the given characteristic of an object.
Alternate: Identify different measuring tools (ruler and yardstick).
- PO 6. *Measure a given object using the appropriate unit of measure:*
- *length – inches, miles,*
 - *capacity/volume – pints, quarts, and*
 - *mass/weight – ounces.*

PO 7. State equivalent relationships:

- 12 inches = 1 foot,
- 60 minutes = 1 hour,
- 24 hours = 1 day,
- 7 days = 1 week,
- 12 months = 1 year,
- 100 pennies = 1 dollar,
- 10 dimes = 1 dollar, and
- 4 quarters = 1 dollar.

Strand 5: Structure and Logic

Concept 1: Algorithms and Algorithmic Thinking

Use reasoning to solve mathematical problems in contextual situations.

PO 1. Create contextual problems that require addition or subtraction with one- or two-digit numbers.

Concept 2: Logic, Reasoning, Arguments, and Mathematical Proof

Evaluate situations, select problem-solving strategies, draw logical conclusions, develop and describe solutions and recognize their applications.

PO 1. Identify the concepts *some*, *every*, and *many* within the context of logical reasoning.
Alternate: Identify the concepts of some and all.

PO 2. Identify the concepts *all* and *none* within the context of logical reasoning.
Alternate: Identify the concepts all and none.

MATHEMATICS STANDARD ARTICULATED BY GRADE LEVEL

Grade 3

Instruction for students identified as having a significant cognitive disability should be developed from Arizona's Alternate Academic Standards. Only those performance objectives that have an identified alternate are required. When developing lessons or activities aligned to the grade level alternate standards, teachers should consider individual student abilities and their need for accommodations, cues, manipulatives/objects, augmentative devices, and communication systems. In addition the depth and breadth of the alternate academic standard can be simplified based on the student's current cognitive abilities. Teachers can also develop lessons using performance objectives without alternates for those students who have developed those specific skills.

Strand 1: Number Sense and Operations

Concept 1: Number Sense	
Understand and apply numbers, ways of representing numbers, the relationships among numbers and different number systems.	
PO 1.	Read whole numbers in contextual situations (through six-digit numbers). Alternate: Identify whole numbers in contextual situations through 50.
PO 2.	Identify six-digit whole numbers in or out of order. Alternate: Identify whole numbers through 50, in or out of order.
PO 3.	Write whole numbers through six-digits in or out of order. Alternate: Write whole numbers 0 through 50, in or out of order.
PO 4.	State whole numbers, through six-digits, with correct place value, by using models, illustrations, symbols, or expanded notation (e.g., $53,941 = 50,000 + 3,000 + 900 + 40 + 1$).
PO 5.	Construct models to represent place value concepts for the one's, ten's, and hundred's places.
PO 6.	Apply expanded notation to model place value through 9,999 (e.g., $5,378 = 5,000 + 300 + 70 + 8$).
PO 7.	Sort whole numbers into sets containing only odd numbers or only even numbers.
PO 8.	Compare two whole numbers, through six-digits.
PO 9.	Order three or more whole numbers through six-digit numbers (least to greatest, or greatest to least). Alternate: Order three whole numbers through 50.
PO 10.	Make models that represent proper fractions (halves, thirds, fourths, eighths, and tenths).

- PO 11. Identify symbols, words, or models that represent proper fractions (halves, thirds, fourths, eighths and tenths).
Alternate: Identify symbols, words, or models that represent halves.
- PO 12. Use proper fractions in contextual situations.
Alternate: Use the proper fraction of halves in contextual situations.
- PO 13. Compare two proper fractions with like denominators.
- PO 14. Order three or more proper fractions with like denominators (halves, thirds, fourths, eighths, and tenths).
- PO 15. Count amounts of money through \$20.00 using pictures or actual bills and coins.
Alternate: Identify penny, nickel, dime, quarter, and dollar by name.
- PO 16. Use decimals through hundredths in contextual situations.
- PO 17. Compare two decimals, through hundredths, using models, illustrations, or symbols.
- PO 18. Order three or more decimals, through hundredths, using models, illustrations, or symbols.
- PO 19. Determine the equivalency among decimals, fractions, and percents (e.g., half-dollar = 50¢ = 50% and $\frac{1}{4} = 0.25 = 25\%$).
Alternate: Identify penny, nickel, dime, quarter, and dollar by value.
- PO 20. Identify whole-number factors and/or pairs of factors for a given whole number through 24.
- PO 21. Determine multiples of a given whole number with products through 24 (skip counting).

Concept 2: Numerical Operations

Understand and apply numerical operations and their relationship to one another.

- PO 1. Demonstrate the process of subtraction using manipulatives through three-digit whole numbers.
Alternate: Demonstrate the process of addition and subtraction.
- PO 2. Add two three-digit whole numbers.
Alternate: Add two one-digit whole numbers.
- PO 3. Subtract two three-digit whole numbers.
Alternate: Subtract two whole numbers through minuends of 10.
- PO 4. Add a column of numbers.
- PO 5. *Select the grade-level appropriate operation to solve word problems.*
- PO 6. *Solve word problems using grade-level appropriate operations and numbers.*
Alternate: Solve word problems using addends and minuends of 10.
- PO 7. Demonstrate the process of multiplication as repeatedly adding the same number, counting by multiples, combining equal sets, and making arrays.
Alternate: Demonstrate the process of multiplication for 2, 5, and 10 as repeatedly adding the same number, counting by multiples and combining equal sets.

- PO 8. Demonstrate the process of division with one-digit divisors (separating elements of a set into smaller equal sets, sharing equally, or repeatedly subtracting the same number).
- PO 9. Demonstrate families of equations for multiplication and division through 9s.
- PO 10. State multiplication and division facts through 9s.
- PO 11. Demonstrate the commutative and identity properties of multiplication.
- PO 12. Identify multiplication and division as inverse operations.
Alternate: Identify addition and subtraction as inverse operations.
- PO 13. *Apply grade-level appropriate properties to assist in computation.*
- PO 14. Apply the symbols: \times , \div , $/$, $*$, $\%$, and the grouping symbols () and “,”.
- PO 15. *Use grade-level appropriate mathematical terminology.*
- PO 16. Add or subtract fractions with like denominators (halves, thirds, fourths, eighths, and tenths) appropriate to grade level.
- PO 17. Apply addition and subtraction in contextual situations, through \$20.00.

Concept 3: Estimation

Use estimation strategies reasonably and fluently.

- PO 1. Solve grade-level appropriate problems using estimation.
Alternate: Estimate in a contextual situation.
- PO 2. Estimate length and weight using U.S. customary units.
- PO 3. Record estimated and actual linear measurements for real-life objects (e.g., length of fingernail; height of desk).
- PO 4. Compare estimations of appropriate measures to the actual measures.
- PO 5. Evaluate the reasonableness of estimated measures.

Strand 2: Data Analysis, Probability, and Discrete Mathematics

Concept 1: Data Analysis (Statistics)

Understand and apply data collection, organization and representation to analyze and sort data.

- PO 1. *Formulate questions to collect data in contextual situations.*
- PO 2. Construct a horizontal bar, vertical bar, pictograph, or tally chart with appropriate labels and title from organized data.
Alternate: Identify a bar graph.
- PO 3. Interpret data found in line plots, pictographs, and single-bar graphs (horizontal and vertical).
- PO 4. Answer questions based on data found in line plots, pictographs, and single-bar graphs (horizontal and vertical).
- PO 5. Formulate questions based on graphs, charts, and tables to solve problems.
- PO 6. *Solve problems using graphs, charts, and tables.*
Alternate: Solve problems using a bar graph.

Concept 2: Probability

Understand and apply the basic concepts of probability.

- PO 1. *Name the possible outcomes for a probability experiment.*
- PO 2. Make predictions about the probability of events being more likely, less likely, equally likely or unlikely.
- PO 3. *Predict the outcome of a grade-level appropriate probability experiment.*
- PO 4. *Record the data from performing a grade-level appropriate probability experiment.*
- PO 5. *Compare the outcome of an experiment to predictions made prior to performing the experiment.*
- PO 6. *Compare the results of two repetitions of the same grade-level appropriate probability experiment.*

Concept 3: Discrete Mathematics – Systematic Listing and Counting

Understand and demonstrate the systematic listing and counting of possible outcomes.

- PO 1. Make a diagram to represent the number of combinations available when 1 item is selected from each of 3 sets of 2 items (e.g., 2 different shirts, 2 different hats, 2 different belts).

Concept 4: Vertex-Edge Graphs

Understand and apply vertex-edge graphs.

- PO 1. *Color maps with the least number of colors so that no common edges share the same color (increased complexity throughout grade levels).*

Strand 3: Patterns, Algebra, and Functions

Concept 1: Patterns

Identify patterns and apply pattern recognition to reason mathematically.

- PO 1. Communicate a grade-level appropriate iterative pattern, using symbols or numbers.
- PO 2. *Extend a grade-level appropriate repetitive pattern* (e.g., 5, 10, 15, 20, . . . rule: add five or count by five's).
Alternate: Extend a pattern of two symbols or numbers.
- PO 3. Solve grade-level appropriate pattern problems.

Concept 2: Functions and Relationships

Describe and model functions and their relationships.

- PO 1. *Describe the rule used in a simple grade-level appropriate function* (e.g., T-chart, input/output model, and frames and arrows).

Concept 3: Algebraic Representations

Represent and analyze mathematical situations and structures using algebraic representations.

- PO 1. *Use variables in contextual situations.*
- PO 2. Solve equations with one variable using missing addends to sums of 18 (e.g., $\square + 9 = 18$, $9 + \square = 18$); and using minuend through 18 (e.g., $18 - \square = 9$, $18 - 9 = \square$).
Alternate: Solve equations with one variable using missing addends to sums of 10 and minuends through 10.

Concept 4: Analysis of Change

Analyze change in a variable over time and in various contexts.

- PO 1. *Identify the change in a variable over time* (e.g., an object gets taller, colder, heavier).
- PO 2. *Make simple predictions based on a variable* (e.g., increases in allowance as you get older).

Strand 4: Geometry and Measurement

Concept 1: Geometric Properties

Analyze the attributes and properties of 2- and 3- dimensional shapes and develop mathematical arguments about their relationships.

- PO 1. Build geometric figures with other common shapes (e.g., tangrams, pattern blocks, geoboards).
- PO 2. Name concrete objects and pictures of 3-dimensional solids (cones, spheres, and cubes).
- PO 3. Describe relationships between 2-dimensional and 3-dimensional objects (squares/cubes, circles/spheres, triangles/cones).
- PO 4. Recognize similar shapes.
Alternate: Recognize shapes (square, circle, triangle, rectangle, and octagon).
- PO 5. Identify a line of symmetry in a 2-dimensional shape.

Concept 2: Transformation of Shapes

Apply spatial reasoning to create transformations and use symmetry to analyze mathematical situations.

- PO 1. *Recognize same shape in different positions (turn/rotation).*

Concept 3: Coordinate Geometry

Specify and describe spatial relationships using coordinate geometry and other representational systems.

- PO 1. Identify points in the first quadrant of a grid using ordered pairs.

Concept 4: Measurement - Units of Measure - Geometric Objects

Understand and apply appropriate units of measure, measurement techniques, and formulas to determine measurements.

- PO 1. Select the appropriate measure of accuracy:
- length – centimeters, meters, kilometers,
 - capacity/volume – liters, and
 - mass/weight – grams.
- PO 2. Tell time with one-minute precision (analog).
Alternate: Tell time to the hour.
- PO 3. Determine the passage of time across months (units of days, weeks, months) using a calendar.
Alternate: Determine the passage of time across one month using a calendar.
- PO 4. *Measure a given object using the appropriate unit of measure:*
- length – centimeters, millimeters, meters, kilometers,
 - capacity/volume – liters, and
 - mass/weight – grams.

PO 5. Record temperatures to the nearest degree in degrees Fahrenheit and degrees Celsius as shown on a thermometer.

PO 6. Compare units of measure to determine more or less relationships for:

- length – inches to feet; centimeters to meters,
- time – minutes to hours; hours to days; days to weeks; months to years, and
- money – pennies, nickels, dimes, quarters, and dollars.

Alternate: Compare units of measure to determine more or less relationships for

- **time – hours to days; days to weeks;**
- **money – pennies, nickels, dimes, quarters, and dollars.**

PO 7. Determine relationships for:

- volume – cups and gallons,
- weight – ounces and pounds, and
- money – extend to amounts greater than one dollar.

PO 8. Compare the length of two objects using U.S. customary or metric units.

Alternate: Compare the length of two objects using inches and feet.

PO 9. Determine the perimeter using a rectangular array.

PO 10. Represent area using a rectangular array.

Strand 5: Structure and Logic

Concept 1: Algorithms and Algorithmic Thinking

Use reasoning to solve mathematical problems in contextual situations.

PO 1. Discriminate necessary information from unnecessary information in a given grade-level appropriate word problem.

Concept 2: Logic, Reasoning, Arguments, and Mathematical Proof

Evaluate situations, select problem-solving strategies, draw logical conclusions, develop and describe solutions and recognize their applications.

PO 1. Draw conclusions based on existing information (e.g., All students in Ms. Dean's 1st grade class are less than 7 years old. Rafael is in Ms. Dean's class. Conclusion: Rafael is less than 7 years old.).

MATHEMATICS STANDARD ARTICULATED BY GRADE LEVEL

Grade 4

Instruction for students identified as having a significant cognitive disability should be developed from Arizona's Alternate Academic Standards. Only those performance objectives that have an identified alternate are required. When developing lessons or activities aligned to the grade level alternate standards, teachers should consider individual student abilities and their need for accommodations, cues, manipulatives/objects, augmentative devices, and communication systems. In addition the depth and breadth of the alternate academic standard can be simplified based on the student's current cognitive abilities. Teachers can also develop lessons using performance objectives without alternates for those students who have developed those specific skills.

Strand 1: Number Sense and Operations

Concept 1: Number Sense	
Understand and apply numbers, ways of representing numbers, the relationships among numbers and different number systems.	
PO 1.	Read whole numbers in contextual situations. Alternate: Identify/match whole numbers in contextual situations.
PO 2.	Identify whole numbers in or out of order. Alternate: Identify/match whole numbers, in or out of order.
PO 3.	Write whole numbers in or out of order. Alternate: Write whole numbers, in or out of order.
PO 4.	State place values for whole numbers (e.g., In the number 203,495 what is the value of the 2?).
PO 5.	Construct models to represent place value concepts for the one's, ten's, hundred's, and thousand's places.
PO 6.	Apply expanded notation to model place value (e.g., $203,495 = 200,000 + 3,000 + 400 + 90 + 5$).
PO 7.	Compare two whole numbers.
PO 8.	Order three or more whole numbers. Alternate: Order five whole numbers.
PO 9.	Make models that represent mixed numbers.
PO 10.	Identify symbols, words, or models that represent mixed numbers. Alternate: Identify symbols, words, or models that represent fourths and halves.
PO 11.	Use mixed numbers in contextual situations. Alternate: Use fourths in contextual situations.
PO 12.	Compare two unit fractions (e.g., $\frac{1}{2}$ to $\frac{1}{5}$) or proper or mixed numbers with like denominators.

- PO 13. Order three or more unit fractions or proper or improper fractions with like denominators.
- PO 14. Use decimals in contextual situations.
Alternate: Use decimals in contextual situations (through hundredths).
- PO 15. Compare two decimals.
- PO 16. Order three or more decimals.
- PO 17. Determine the equivalency among decimals, fractions, and percents (e.g., $49/100 = 0.49 = 49\%$).
- PO 18. Identify all whole number factors and pairs of factors for a given whole number through 144.
- PO 19. Determine multiples of a given whole number with products through 144.

Concept 2: Numerical Operations

Understand and apply numerical operations and their relationship to one another.

- PO 1. Add whole numbers.
Alternate: Add whole numbers using addends up to 50.
- PO 2. Subtract whole numbers.
Alternate: Subtract whole numbers using minuends up to 25.
- PO 3. *Select the grade-level appropriate operation to solve word problems.*
- PO 4. *Solve word problems using grade-level appropriate operations and numbers.*
Alternate: Solve word problems using addends and minuends to 25.
- PO 5. Multiply multi-digit numbers by two-digit numbers.
- PO 6. Divide with one-digit divisors.
- PO 7. State multiplication and division facts through 12s.
Alternate: Use multiplication tables for facts through 10s.
- PO 8. Demonstrate the associative property of multiplication.
- PO 9. *Apply grade-level appropriate properties to assist in computation.*
- PO 10. Apply the symbol: \bullet and $()$ for multiplication, and \leq, \geq .
- PO 11. *Use grade-level appropriate mathematical terminology.*
- PO 12. Add or subtract fractions with like denominators, no regrouping.
- PO 13. Simplify numerical expressions using the order of operations with grade-appropriate operations on number sets.

Concept 3: Estimation

Use estimation strategies reasonably and fluently.

- PO 1. *Solve grade-level appropriate problems using estimation.*
Alternate: Solve problems using estimation in contextual situations.
- PO 2. Use estimation to verify the reasonableness of a calculation (e.g., Is $3284 \times 343 = 1200$ reasonable?).
- PO 3. Estimate length and weight using both U.S. customary and metric units.
- PO 4. Estimate and measure for distance.

Strand 2: Data Analysis, Probability, and Discrete Mathematics

Concept 1: Data Analysis (Statistics)

Understand and apply data collection, organization and representation to analyze and sort data.

- PO 1. *Formulate questions to collect data in contextual situations.*
- PO 2. Construct a single-bar graph, line graph or two-set Venn diagram with appropriate labels and title from organized data.
Alternate: Identify a bar graph and a circle graph.
- PO 3. Interpret graphical representations and data displays including single-bar graphs, circle graphs, two-set Venn diagrams, and line graphs that display continuous data.
- PO 4. Answer questions based on graphical representations and data displays including single-bar graphs, circle graphs, two-set Venn diagrams, and line graphs that display continuous data.
- PO 5. Identify the mode(s) of given data.
- PO 6. Formulate predictions from a given set of data.
- PO 7. Solve contextual problems using graphs, charts, and tables.
Alternate: Solve problems using bar graphs and circle graphs.

Concept 2: Probability

Understand and apply the basic concepts of probability.

- PO 1. *Name the possible outcomes for a probability experiment.*
- PO 2. Describe the probability of events as being more likely, less likely, equally likely, unlikely, certain, impossible, fair or unfair.
Alternate: Describe the probability of events as being certain or impossible.
- PO 3. *Predict the outcome of a grade-level appropriate probability experiment.*
- PO 4. *Record the data from performing a grade-level appropriate probability experiment.*
- PO 5. *Compare the outcome of an experiment to predictions made prior to performing the experiment.*
- PO 6. Make predictions from the results of student-generated experiments using objects (e.g., coins, spinners, number cubes).
- PO 7. *Compare the results of two repetitions of the same grade-level appropriate probability experiment.*

Concept 3: Discrete Mathematics – Systematic Listing and Counting

Understand and demonstrate the systematic listing and counting of possible outcomes.

PO 1. Find all possible combinations when one item is selected from each of two sets containing up to three objects (e.g., How many outfits can be made with 3 pants and 2 tee shirts?).

Concept 4: Vertex-Edge Graphs

Understand and apply vertex-edge graphs.

PO 1. *Color maps with the least number of colors so that no common edges share the same color (increased complexity throughout grade levels).*

Strand 3: Patterns, Algebra, and Functions

Concept 1: Patterns

Identify patterns and apply pattern recognition to reason mathematically.

PO 1. *Communicate a grade-level appropriate iterative pattern, using symbols or numbers.*

PO 2. Extend a grade-level appropriate iterative pattern.
Alternate: Extend a pattern.

PO 3. Create grade-level appropriate iterative patterns.

Concept 2: Functions and Relationships

Describe and model functions and their relationships.

PO 1. *Describe the rule used in a simple grade-level appropriate function (e.g., T-chart, input/output model).*

Concept 3: Algebraic Representations

Represent and analyze mathematical situations and structures using algebraic representations.

PO 1. Evaluate expressions involving the four basic operations by substituting given whole numbers for the variable.

PO 2. *Use variables in contextual situations.*
Alternate: Use variables in contextual situations.

PO 3. Solve one-step equations with one variable represented by a letter or symbol using multiplication of whole numbers (e.g., $12 = n \times 4$).
Alternate: Solve equations with one variable using missing addends to sums of 20 and using minuends through 20.

Concept 4: Analysis of Change

Analyze change in a variable over time and in various contexts.

PO 1. *Identify the change in a variable over time (e.g., an object gets taller, colder, heavier).*

PO 2. *Make simple predictions based on a variable (e.g., increase homework time as you progress through the grades).*

Strand 4: Geometry and Measurement

Concept 1: Geometric Properties

Analyze the attributes and properties of 2- and 3- dimensional shapes and develop mathematical arguments about their relationships.

- PO 1. Identify the properties of 2-dimensional figures using appropriate terminology.
- PO 2. Identify models or illustrations of prisms, pyramids, cones, cylinders, and spheres.
Alternate: Identify pyramids, cones, cylinders, and spheres.
- PO 3. Draw points, lines, line segments (open or closed endpoints), rays, or angles.
- PO 4. Classify angles (e.g., right, acute, obtuse, straight).
- PO 5. Classify triangles as right, acute, or obtuse.
- PO 6. Identify congruent geometric shapes.
- PO 7. Identify similar shapes.
Alternate: Identify similar shapes.
- PO 8. Draw a 2-dimensional shape that has line symmetry.

Concept 2: Transformation of Shapes

Apply spatial reasoning to create transformations and use symmetry to analyze mathematical situations.

- PO 1. Demonstrate translation using geometric figures.
- PO 2. Identify a tessellation.

Concept 3: Coordinate Geometry

Specify and describe spatial relationships using coordinate geometry and other representational systems.

- PO 1. Name the coordinates of a point plotted in the first quadrant.

Concept 4: Measurement - Units of Measure - Geometric Objects

Understand and apply appropriate units of measure, measurement techniques, and formulas to determine measurements.

- PO 1. Identify the appropriate measure of accuracy for the area of an object (e.g., sq. feet or sq. miles).
- PO 2. Compute elapsed time using a clock (e.g., hours and minutes since or until...) or a calendar (e.g., days, weeks, years since or until...)
Alternate: Tell time to the half hour.
- PO 3. Select an appropriate tool to use in a particular measurement situation.
Alternate: Identify an appropriate tool to use in a particular measurement situation.
- PO 4. Approximate measurements to the appropriate degree of accuracy.

- PO 5. Compare units of measure to determine *more* or *less* relationships including:
- length - yards and miles, meters and kilometers, and
 - weight - pounds and tons, grams and kilograms.
- PO 6. State equivalent relationships (e.g., 3 teaspoons = 1 tablespoon, 16 cups = 1 gallon, 2000 pounds = 1 ton).
Alternate: Identify equivalent relationships (12 inches=1 foot, 60 minutes=1 hour, 24 hours=1 day, and 7 days=1 week).
- PO 7. Compare the weight of two objects using both U.S. customary and metric units.
Alternate: Compare the length of two objects using inches to feet and feet to yards.
- PO 8. Determine the perimeter of simple polygons (e.g., square, rectangle, triangle).
- PO 9. Determine the area of squares and rectangles.
- PO 10. Differentiate between perimeter and area of quadrilaterals.

Strand 5: Structure and Logic

Concept 1: Algorithms and Algorithmic Thinking

Use reasoning to solve mathematical problems in contextual situations.

PO 1. *Discriminate necessary information from unnecessary information in a given grade-level appropriate word problem.*

PO 2. Develop an algorithm to calculate the perimeter of simple polygons.

Concept 2: Logic, Reasoning, Arguments, and Mathematical Proof

Evaluate situations, select problem-solving strategies, draw logical conclusions, develop and describe solutions and recognize their applications.

PO 1. Draw a conclusion from a Venn diagram.

Alternate: Draw a conclusion from bar graphs or circle graphs.

PO 2. Identify simple valid arguments using *if...then* statements based on graphic organizers (e.g., 2-set Venn diagrams and pictures).

MATHEMATICS STANDARD ARTICULATED BY GRADE LEVEL

Grade 5

Instruction for students identified as having a significant cognitive disability should be developed from Arizona's Alternate Academic Standards. Only those performance objectives that have an identified alternate are required. When developing lessons or activities aligned to the grade level alternate standards, teachers should consider individual student abilities and their need for accommodations, cues, manipulatives/objects, augmentative devices, and communication systems. In addition the depth and breadth of the alternate academic standard can be simplified based on the student's current cognitive abilities. Teachers can also develop lessons using performance objectives without alternates for those students who have developed those specific skills.

Strand 1: Number Sense and Operations

Concept 1: Number Sense	
Understand and apply numbers, ways of representing numbers, the relationships among numbers and different number systems.	
PO 1.	Make models that represent improper fractions.
PO 2.	Identify symbols, words, or models that represent improper fractions. Alternate: Identify fourths, thirds, and halves.
PO 3.	Use improper fractions in contextual situations. Alternate: Use thirds in contextual situations.
PO 4.	Compare two proper fractions or improper fractions with like denominators.
PO 5.	Order three or more unit fractions, proper or improper fractions with like denominators, or mixed numbers with like denominators.
PO 6.	Compare two whole numbers, fractions, and decimals (e.g., $1/2$ to 0.6). Alternate: Compare two whole numbers or fractions.
PO 7.	Order whole numbers, fractions, and decimals. Alternate: Order whole numbers or fractions.
PO 8.	Determine the equivalency between and among fractions, decimals, and percents in contextual situations.
PO 9.	Identify all whole number factors and pairs of factors for a number.
PO 10.	Recognize that 1 is neither a prime nor a composite number.
PO 11.	Sort whole numbers (through 50) into sets containing only prime numbers or only composite numbers.

Concept 2: Numerical Operations

Understand and apply numerical operations and their relationship to one another.

- PO 1. *Select the grade-level appropriate operation to solve word problems.*
Alternate: Select the operation of addition or subtraction to solve word problems.
- PO 2. *Solve word problems using grade-level appropriate operations and numbers.*
Alternate: Solve word problems using addends and minuends to 50.
- PO 3. Multiply whole numbers.
Alternate: Multiply whole numbers through 10.
- PO 4. Divide with whole numbers.
- PO 5. Demonstrate the distributive property of multiplication over addition.
- PO 6. Demonstrate the addition and multiplication properties of equality.
- PO 7. *Apply grade-level appropriate properties to assist in computation.*
- PO 8. Apply the symbol “[]” to represent grouping.
- PO 9. *Use grade-level appropriate mathematical terminology.*
- PO 10. Simplify fractions to lowest terms.
- PO 11. Add or subtract proper fractions and mixed numbers with like denominators with regrouping.
Alternate: Add fractions with like denominators of 2, 3, or 4.
- PO 12. Add or subtract decimals.
Alternate: Add and subtract decimals to the hundredths.
- PO 13. Multiply decimals.
- PO 14. Divide decimals.
- PO 15. *Simplify numerical expressions using the order of operations with grade- appropriate operations on number sets.*

Concept 3: Estimation

Use estimation strategies reasonably and fluently.

- PO 1. Solve grade-level appropriate problems using estimation.
Alternate: Solve problems using estimation in contextual situations.
- PO 2. *Use estimation to verify the reasonableness of a calculation (e.g., Is 4.1×2.7 about 12?).*
- PO 3. Round to estimate quantities.
Alternate: Round whole numbers to nearest tens or to the nearest hundreds.
- PO 4. Estimate and measure for area and perimeter.
- PO 5. Compare estimated measurements between U.S. customary and metric systems (e.g., A yard is about a meter.).

Strand 2: Data Analysis, Probability, and Discrete Mathematics

Concept 1: Data Analysis (Statistics)

Understand and apply data collection, organization and representation to analyze and sort data.

- PO 1. *Formulate questions to collect data in contextual situations.*
- PO 2. Construct a double-bar graph, line plot, frequency table, or three-set Venn diagram with appropriate labels and title from organized data.
Alternate: Construct a pictograph or bar graph with appropriate labels.
- PO 3. Interpret graphical representations and data displays including bar graphs (including double-bar), circle graphs, frequency tables, three-set Venn diagrams, and line graphs that display continuous data.
- PO 4. Answer questions based on graphical representations, and data displays including bar graphs (including double-bar), circle graphs, frequency tables, three-set Venn diagrams, and line graphs that display continuous data.
- PO 5. Identify the mode(s) and mean (average) of given data.
- PO 6. Formulate reasonable predictions from a given set of data.
- PO 7. Compare two sets of data related to the same investigation.
- PO 8. *Solve contextual problems using graphs, charts, and tables.*
Alternate: Solve problems using bar graphs, line graphs, and circle graphs.

Concept 2: Probability

Understand and apply the basic concepts of probability.

- PO 1. *Name the possible outcomes for a probability experiment.*
- PO 2. Describe the probability of events as being:
 - certain (represented by “1”),
 - impossible, (represented by “0”), or
 - neither certain nor impossible (represented by a fraction less than 1).**Alternate: Describe the probability of events as being certain, impossible, more likely or less likely.**
- PO 3. *Predict the outcome of a grade-level appropriate probability experiment.*
- PO 4. *Record the data from performing a grade-level appropriate probability experiment.*
Alternate: Record the data from a probability experiment.
- PO 5. *Compare the outcome of an experiment to predictions made prior to performing the experiment.*
- PO 6. *Make predictions from the results of student-generated experiments using objects (e.g., coins, spinners, number cubes).*
- PO 7. *Compare the results of two repetitions of the same grade-level appropriate probability experiment.*

Concept 3: Discrete Mathematics – Systematic Listing and Counting

Understand and demonstrate the systematic listing and counting of possible outcomes.

PO 1. Find all possible combinations when one item is selected from each of two sets of different items, using a systematic approach. (e.g., shirts: tee shirt, tank top, sweatshirt; pants: shorts, jeans).

Concept 4: Vertex-Edge Graphs

Understand and apply vertex-edge graphs.

PO 1. *Color maps with the least number of colors so that no common edges share the same color (increased complexity throughout grade levels).*

Strand 3: Patterns, Algebra, and Functions

Concept 1: Patterns

Identify patterns and apply pattern recognition to reason mathematically.

PO 1. *Communicate a grade-level appropriate iterative pattern, using symbols or numbers.*

PO 2. *Extend a grade-level appropriate iterative pattern.*

Alternate: Extend a pattern of 3 or more symbols or numbers.

PO 3. Solve grade-level appropriate iterative pattern problems.

Concept 2: Functions and Relationships

Describe and model functions and their relationships.

PO 1. *Describe the rule used in a simple grade-level appropriate function (e.g., T-chart, input/output model).*

Concept 3: Algebraic Representations

Represent and analyze mathematical situations and structures using algebraic representations.

PO 1. Evaluate expressions involving the four basic operations by substituting given decimals for the variable.

PO 2. *Use variables in contextual situations.*

Alternate: Use variables in contextual situations.

PO 3. Solve one-step equations with one variable represented by a letter or symbol (e.g., $15 = 45 \div n$).

Alternate: Solve equations with one variable using missing addends to sums of 50 and using minuends to 50.

Concept 4: Analysis of Change

Analyze change in a variable over time and in various contexts.

PO 1. Describe patterns of change:

- constant rate (speed of movement of the hands on a clock), and
- increasing or decreasing rate (rate of plant growth).

Strand 4: Geometry and Measurement

Concept 1: Geometric Properties

Analyze the attributes and properties of 2- and 3- dimensional shapes and develop mathematical arguments about their relationships.

- PO 1. Recognize regular polygons.
- PO 2. Draw 2-dimensional figures by applying significant properties of each (e.g., Draw a quadrilateral with two sets of parallel sides and four right angles.).
- PO 3. Sketch prisms, pyramids, cones, and cylinders.
Alternate: Identify pyramids, cones, cylinders, and spheres in contextual situations.
- PO 4. Identify the properties of 2- and 3-dimensional geometric figures using appropriate terminology and vocabulary.
- PO 5. Draw points, lines, line segments, rays, and angles with appropriate labels.
Alternate: Identify points, lines, and angles.
- PO 6. Recognize that all pairs of vertical angles are congruent.
- PO 7. Classify triangles as scalene, isosceles, or equilateral.
- PO 8. Recognize that a circle is a 360° rotation about a point.
- PO 9. Identify the diameter, radius, and circumference of a circle.
- PO 10. Understand that the sum of the angles of a triangle is 180° .
- PO 11. Draw two congruent geometric figures.
Alternate: Identify two similar geometric figures.
- PO 12. Draw two similar geometric figures.
- PO 13. Identify the lines of symmetry in a 2-dimensional shape.

Concept 2: Transformation of Shapes

Apply spatial reasoning to create transformations and use symmetry to analyze mathematical situations.

- PO 1. Demonstrate reflections using geometric figures.
- PO 2. Describe the transformations that created a tessellation.

Concept 3: Coordinate Geometry

Specify and describe spatial relationships using coordinate geometry and other representational systems.

- PO 1. Graph points in the first quadrant on a grid using ordered pairs.

Concept 4: Measurement - Units of Measure - Geometric Objects

Understand and apply appropriate units of measure, measurement techniques, and formulas to determine measurements.

- PO 1. State an appropriate measure of accuracy for a contextual situation (e.g., What unit of measurement would you use to measure the top of your desk?).
Alternate: Identify an appropriate measure of accuracy for a contextual situation.
- PO 2. Draw 2-dimensional figures to specifications using the appropriate tools (e.g., Draw a circle with a 2-inch radius.).
- PO 3. Determine relationships including volume (e.g., pints and quarts, milliliters and liters).
Alternate: Identify tools used for measuring liquids (cups and gallons).
- PO 4. Convert measurement units to equivalent units within a given system (U.S. customary and metric) (e.g., 12 inches = 1 foot; 10 decimeters = 1 meter).
- PO 5. Solve problems involving the perimeter of convex polygons.
Alternate: Identify the perimeter of objects.
- PO 6. Determine the area of figures composed of two or more rectangles on a grid.
- PO 7. Solve problems involving the area of simple polygons.
- PO 8. Describe the change in perimeter or area when one attribute (length, width) of a rectangle is altered.

Strand 5: Structure and Logic

Concept 1: Algorithms and Algorithmic Thinking

Use reasoning to solve mathematical problems in contextual situations.

- PO 1. *Discriminate necessary information from unnecessary information in a given grade-level appropriate word problem.*
- PO 2. Design simple algorithms using whole numbers.
- PO 3. Develop an algorithm or formula to calculate areas of simple polygons.

Concept 2: Logic, Reasoning, Arguments, and Mathematical Proof

Evaluate situations, select problem-solving strategies, draw logical conclusions, develop and describe solutions and recognize their applications.

- PO 1. Construct *if...then* statements.
Alternate: Construct *if.....then* statements.
- PO 2. *Identify simple valid arguments using if ... then statements based on graphic organizers (e.g., 3-set Venn diagrams and pictures).*

MATHEMATICS STANDARD ARTICULATED BY GRADE LEVEL

Grade 6

Instruction for students identified as having a significant cognitive disability should be developed from Arizona's Alternate Academic Standards. Only those performance objectives that have an identified alternate are required. When developing lessons or activities aligned to the grade level alternate standards, teachers should consider individual student abilities and their need for accommodations, cues, manipulatives/objects, augmentative devices, and communication systems. In addition the depth and breadth of the alternate academic standard can be simplified based on the student's current cognitive abilities. Teachers can also develop lessons using performance objectives without alternates for those students who have developed those specific skills.

Strand 1: Number Sense and Operations

Concept 1: Number Sense	
Understand and apply numbers, ways of representing numbers, the relationships among numbers and different number systems.	
PO 1.	Express fractions as ratios, comparing two whole numbers (e.g., $\frac{3}{4}$ is equivalent to 3:4 and 3 to 4).
PO 2.	Compare two proper fractions, improper fractions, or mixed numbers. Alternate: Compare two proper fractions.
PO 3.	Order three or more proper fractions, improper fractions, or mixed numbers. Alternate: Order three or more proper fractions.
PO 4.	Determine the equivalency between and among fractions, decimals, and percents in contextual situations. Alternate: Determine the relationship between fractions and decimals (equal, more, or less).
PO 5.	Identify the greatest common factor for two whole numbers.
PO 6.	Determine the least common multiple for two whole numbers.
PO 7.	Express a whole number as a product of its prime factors, using exponents when appropriate.

Concept 2: Numerical Operations	
Understand and apply numerical operations and their relationship to one another.	
PO 1.	<i>Select the grade-level appropriate operation to solve word problems.</i> Alternate: Select addition, subtraction, or multiplication to solve word problems.
PO 2.	<i>Solve word problems using grade-level appropriate operations and numbers.</i> Alternate: Solve word problems using addition, subtraction, or multiplication through 10.
PO 3.	<i>Apply grade-level appropriate properties to assist in computation.</i>

- PO 4. Apply the symbols for “...” or “ $\overline{\quad}$ ” to represent repeating decimals and “:” to represent ratios, superscripts as exponents.
- PO 5. *Use grade-level appropriate mathematical terminology.*
- PO 6. *Simplify fractions to lowest terms.*
- PO 7. Add or subtract proper fractions and mixed numbers with unlike denominators with regrouping.
Alternate: Add or subtract proper fractions with like denominators.
- PO 8. Demonstrate the process of multiplication of proper fractions using models.
- PO 9. Multiply proper fractions.
- PO 10. Multiply mixed numbers.
- PO 11. Demonstrate that division is the inverse of multiplication of proper fractions.
Alternate: Demonstrate that division is the inverse of multiplication.
- PO 12. Divide proper fractions.
- PO 13. Divide mixed numbers.
- PO 14. Solve problems involving fractions or decimals (including money) in contextual situations.
Alternate: Solve problems involving fractions or decimals (including money) in contextual situations.
- PO 15. Simplify numerical expressions using the order of operations with grade-appropriate operations on number sets.

Concept 3: Estimation

Use estimation strategies reasonably and fluently.

- PO 1. *Solve grade-level appropriate problems using estimation.*
Alternate: Solve problems using estimation in contextual situations.
- PO 2. *Use estimation to verify the reasonableness of a calculation (e.g., Is $5/9 \times 3/7$ more than 1?).*
- PO 3. Round to estimate quantities in contextual situations (e.g., round up or round down).
Alternate: Round whole numbers to the nearest tens or hundreds in contextual situations.
- PO 4. Estimate and measure for the area and perimeter of polygons using a grid.
Alternate: Estimate perimeter.
- PO 5. Verify the reasonableness of estimates made from calculator results within a contextual situation.
Alternate: Estimate and check on a calculator.

Strand 2: Data Analysis, Probability, and Discrete Mathematics

Concept 1: Data Analysis (Statistics)

Understand and apply data collection, organization and representation to analyze and sort data.

- PO 1. *Formulate questions to collect data in contextual situations.*
- PO 2. Construct a histogram, line graph, scatter plot, or stem-and-leaf plot with appropriate labels and title from organized data.
Alternate: Construct bar graphs, tally charts, line graphs, circle graphs, or Venn diagrams with appropriate labels.
- PO 3. Interpret simple displays of data including double bar graphs, tally charts, frequency tables, circle graphs, and line graphs.
Alternate: Interpret simple displays of data for bar graphs, tally charts, line graphs, circle graphs or Venn diagrams.
- PO 4. Answer questions based on simple displays of data including double bar graphs, tally charts, frequency tables, circle graphs, and line graphs.
- PO 5. Find the mean, median (odd number of data points), mode, range, and extreme values of a given numerical data set.
- PO 6. Identify a trend (variable increasing, decreasing, remaining constant) from displayed data.
- PO 7. Compare trends in data related to the same investigation.
- PO 8. Solve contextual problems using bar graphs, tally charts, and frequency tables.
Alternate: Solve problems using bar graphs, tally charts, line graphs, circle graphs, or Venn diagrams.

Concept 2: Probability

Understand and apply the basic concepts of probability.

- PO 1. *Name the possible outcomes for a probability experiment.*
- PO 2. Express probabilities of a single event as a decimal.
- PO 3. *Predict the outcome of a grade-level appropriate probability experiment.*
Alternate: Predict an outcome of a probability experiment.
- PO 4. *Record the data from performing a grade-level appropriate probability experiment.*
Alternate: Record the data from a probability experiment.
- PO 5. *Compare the outcome of an experiment to predictions made prior to performing the experiment.*
Alternate: Compare the outcome of an experiment to predictions made prior to performing the experiment.
- PO 6. *Make predictions from the results of student-generated experiments using objects (e.g., coins, spinners, number cubes, cards).*
- PO 7. *Compare the results of two repetitions of the same grade-level appropriate probability experiment.*

Concept 3: Discrete Mathematics – Systematic Listing and Counting

Understand and demonstrate the systematic listing and counting of possible outcomes.

- PO 1. Determine all possible outcomes involving a combination of three sets of three items, using a systematic approach (e.g., 3 different shirts, 3 different pairs of pants, and 3 different belts).
- PO 2. Determine all possible arrangements given a set with four or fewer objects using a systematic list, table or tree diagram when order is not important.

Concept 4: Vertex-Edge Graphs

Understand and apply vertex-edge graphs.

- PO 1. Find the shortest route on a map from one site to another (vertex-edge graph).

Alternate: Find the shortest route on a map from one site to another.

Strand 3: Patterns, Algebra, and Functions

Concept 1: Patterns

Identify patterns and apply pattern recognition to reason mathematically.

PO 1. Communicate a grade-level appropriate recursive pattern, using symbols or numbers.

Alternate: Identify the rule for a pattern of symbols or numbers.

PO 2. *Extend a grade-level appropriate iterative pattern.*

Alternate: Extend a pattern using symbols or numbers.

PO 3. *Solve grade-level appropriate iterative pattern problems.*

Concept 2: Functions and Relationships

Describe and model functions and their relationships.

PO 1. *Describe the rule used in a simple grade-level appropriate function (e.g., T-chart, input/output model).*

Concept 3: Algebraic Representations

Represent and analyze mathematical situations and structures using algebraic representations.

PO 1. Evaluate expressions involving the four basic operations by substituting given fractions for the variable (e.g., $n+3$, when $n = \frac{1}{2}$).

Alternate: Evaluate expressions involving addition or subtraction by substituting given whole numbers for the variable.

PO 2. *Use variables in contextual situations.*

Alternate: Use variables in contextual situations.

PO 3. Translate a written phrase to an algebraic expression (e.g., The quotient of m and 5 is $\frac{m}{5}$ or $m \div 5$).

PO 4. Translate a phrase written in context into an algebraic expression (e.g., Write an expression to describe the situation: John has x pieces of candy and buys three more. $x + 3$).

PO 5. Solve one-step equations with one variable represented by a letter or symbol, using inverse operations with whole numbers.

Concept 4: Analysis of Change

Analyze change in a variable over time and in various contexts.

PO 1. Identify values on a given line graph or scatter plot (e.g., Given a line showing wages earned per hour, what is the wage at five hours?).

Strand 4: Geometry and Measurement

Concept 1: Geometric Properties

Analyze the attributes and properties of 2- and 3- dimensional shapes and develop mathematical arguments about their relationships.

- PO 1. Classify polygons by their attributes (e.g., number of sides, length of sides, angles, parallelism, perpendicularity).
Alternate: Classify shapes and figures by their attributes.
- PO 2. Draw a geometric figure showing specified properties, such as parallelism and perpendicularity.
- PO 3. Classify prisms, pyramids, cones, and cylinders by base shape and lateral surface shape.
- PO 4. Classify 3-dimensional figures by their attributes.
- PO 5. Compare attributes of 2-dimensional figures with 3-dimensional figures.
- PO 6. Draw triangles with appropriate labels.
- PO 7. Identify supplementary or complementary angles.
- PO 8. Identify the diameter, radius, and circumference of a circle or sphere.
Alternate: Identify the circumference of circles or spheres.
- PO 9. Draw a 2-dimensional shape with a given number of lines of symmetry.

Concept 2: Transformation of Shapes

Apply spatial reasoning to create transformations and use symmetry to analyze mathematical situations.

- PO 1. Identify reflections and translations using pictures.
- PO 2. Perform elementary transformations to create a tessellation.

Concept 3: Coordinate Geometry

Specify and describe spatial relationships using coordinate geometry and other representational systems.

- PO 1. Graph a polygon in the first quadrant using ordered pairs.
- PO 2. State the missing coordinate of a given figure in the first quadrant of a coordinate grid using geometric properties (e.g., Find the coordinates of the missing vertex of a rectangle when two adjacent sides are drawn.).

Concept 4: Measurement - Units of Measure - Geometric Objects

Understand and apply appropriate units of measure, measurement techniques, and formulas to determine measurements.

- PO 1. Determine the appropriate measure of accuracy within a system for a given contextual situation
(e.g., Would you measure the length of your bedroom wall using inches or feet?).
Alternate: Identify an appropriate measure of accuracy for a given contextual situation.
- PO 2. Determine the appropriate tool needed to measure to the needed accuracy.
Alternate: Identify the appropriate tool needed to measure for accuracy.
- PO 3. Determine a linear measurement to the appropriate degree of accuracy.
- PO 4. Measure angles using a protractor.
- PO 5. Convert within a single measurement system (U.S. customary or metric) (e.g., How many ounces are equivalent to 2 pounds?).
- PO 6. Solve problems involving the perimeter of polygons.
Alternate: Find perimeter of an object.
- PO 7. Determine the area of triangles.
Alternate: Identify the area of a simple polygon.
- PO 8. Distinguish between perimeter and area in contextual situation.
- PO 9. Solve problems for the areas of parallelograms (includes rectangles).
- PO 10. Identify parallelograms having the same perimeter or area.
- PO 11. Determine the actual measure of objects using a scale drawing or map.
Alternate: Determine the actual measurements of objects.

Strand 5: Structure and Logic

Concept 1: Algorithms and Algorithmic Thinking

Use reasoning to solve mathematical problems in contextual situations.

PO 1. *Discriminate necessary information from unnecessary information in a given grade-level appropriate word problem.*

PO 2. Analyze algorithms for computing with decimals.

Concept 2: Logic, Reasoning, Arguments, and Mathematical Proof

Evaluate situations, select problem-solving strategies, draw logical conclusions, develop and describe solutions and recognize their applications.

PO 1. Solve a simple logic problem from given information (e.g., Which of three different people live in which of three different colored houses?).

Alternate: Solve a simple logic problem from given information.

MATHEMATICS STANDARD ARTICULATED BY GRADE LEVEL

Grade 7

Instruction for students identified as having a significant cognitive disability should be developed from Arizona's Alternate Academic Standards. Only those performance objectives that have an identified alternate are required. When developing lessons or activities aligned to the grade level alternate standards, teachers should consider individual student abilities and their need for accommodations, cues, manipulatives/objects, augmentative devices, and communication systems. In addition the depth and breadth of the alternate academic standard can be simplified based on the student's current cognitive abilities. Teachers can also develop lessons using performance objectives without alternates for those students who have developed those specific skills.

Strand 1: Number Sense and Operations

Concept 1: Number Sense	
Understand and apply numbers, ways of representing numbers, the relationships among numbers and different number systems.	
PO 1.	Express fractions as terminating or repeating decimals.
PO 2.	Identify the greatest common factor for a set of whole numbers.
PO 3.	Determine the least common multiple for a set of whole numbers.
PO 4.	Choose the appropriate signed real number to represent a contextual situation.
PO 5.	Recognize the absolute value of a number used in contextual situations.
PO 6.	Locate integers on a number line. Alternate: Locate whole numbers (positive and negative) on a number line.
PO 7.	Order integers. Alternate: Order whole numbers (positive and negative).
PO 8.	Classify rational numbers as natural, whole, or integers.

Concept 2: Numerical Operations	
Understand and apply numerical operations and their relationship to one another.	
PO 1.	Add integers.
PO 2.	Subtract integers.
PO 3.	<i>Select the grade-level appropriate operation to solve word problems.</i> Alternate: Select the appropriate operation of addition, subtraction, or multiplication to solve word problems.
PO 4.	<i>Solve word problems using grade-level appropriate operations and numbers.</i> Alternate: Solve word problems using addition, subtraction or multiplication.

- PO 5. Multiply integers.
- PO 6. Divide integers.
Alternate: Divide whole numbers with a one-digit divisor.
- PO 7. *Apply grade-level appropriate properties to assist in computation.*
- PO 8. Apply the symbols + and – to represent positive and negative, and “| |” to represent absolute value.
Alternate: Apply the symbols + and – to represent positive and negative in contextual situations.
- PO 9. *Use grade-level appropriate mathematical terminology.*
- PO 10. Calculate the percent of a given number.
- PO 11. Convert numbers expressed in standard notation to scientific notation and vice versa (positive exponents only).
- PO 12. *Simplify numerical expressions using the order of operations with grade- appropriate operations on number sets.*

Concept 3: Estimation

Use estimation strategies reasonably and fluently.

- PO 1. *Solve grade-level appropriate problems using estimation.*
Alternate: Solve problems using estimation in a contextual situation.
- PO 2. *Use estimation to verify the reasonableness of a calculation (e.g., Is -2.5×18 about -50 ?).*
- PO 3. Determine whether an estimation of an area is approximately equal to the actual measure.
- PO 4. Determine whether an estimation of an angle is approximately equal to the actual measure.
- PO 5. Determine whether an estimation of the circumference of a circle is approximately equal to the actual measure.
- PO 6. *Verify the reasonableness of estimates made from calculator results within a contextual situation.*
Alternate: Estimate and check on a calculator.

Strand 2: Data Analysis, Probability, and Discrete Mathematics

Concept 1: Data Analysis (Statistics)

Understand and apply data collection, organization and representation to analyze and sort data.

- PO 1. *Formulate questions to collect data in contextual situations.*
- PO 2. Construct a circle graph with appropriate labels and title from organized data.
Alternate: Construct bar graphs, tally charts, line graphs, circle graphs, or Venn diagrams with appropriate labels.
- PO 3. Determine when it is appropriate to use histograms, line graphs, double bar graphs, and stem-and-leaf plots.
- PO 4. Interpret data displays including histograms, stem-and-leaf plots, circle graphs, and double line graphs.
Alternate: Interpret simple displays of data including bar graphs, tally charts, line graphs, circle graphs or Venn diagrams.
- PO 5. Answer questions based on data displays including histograms, stem-and-leaf plots, circle graphs, and double line graphs.
- PO 6. Find the mean, median, mode, and range of a given numerical data set.
- PO 7. Interpret trends from displayed data.
- PO 8. Compare trends in data related to the same investigation.
- PO 9. Solve contextual problems using histograms, line graphs of continuous data, double bar graphs, and stem-and-leaf plots.
Alternate: Solve problems using bar graphs, tally charts, line graphs, circle graphs, or Venn diagrams.

Concept 2: Probability

Understand and apply the basic concepts of probability.

- PO 1. Determine the probability that a specific event will occur in a single stage probability experiment (e.g., Find the probability of drawing a red marble from a bag with 3 red, 5 blue, and 9 black marbles.).
- PO 2. Compare probabilities to determine the fairness of a contextual situation (e.g. If John wins when two or greater shows after a six-sided number cube is rolled and Joaquin wins otherwise, is this a fair game?).
- PO 3. *Predict the outcome of a grade-level appropriate probability experiment.*
Alternate: Predict the outcome of a probability experiment.
- PO 4. *Record the data from performing a grade-level appropriate probability experiment.*
Alternate: Record the data from a probability experiment.
- PO 5. *Compare the outcome of an experiment to predictions made prior to performing the experiment.*
Alternate: Compare the outcome of an experiment to predictions made prior to performing the experiment.

- PO 6. Make predictions from the results of student-generated experiments using objects (e.g., coins, spinners, number cubes, cards).
Alternate: Make predictions from the results of student-generated experiments using objects.
- PO 7. *Compare the results of two repetitions of the same grade-level appropriate probability experiment.*

Concept 3: Discrete Mathematics – Systematic Listing and Counting

Understand and demonstrate the systematic listing and counting of possible outcomes.

- PO 1. Determine all possible outcomes involving the combination of up to three sets of objects (e.g., How many outfits can be made with 3 pants, 2 tee shirts and 2 pairs of shoes?).
- PO 2. Determine all possible arrangements of a given set, using a systematic list, table, tree diagram, or other representation.

Concept 4: Vertex-Edge Graphs

Understand and apply vertex-edge graphs.

- PO 1. Find the shortest circuit on a map that makes a tour of specified sites (vertex-edge graph).
Alternate: Find the shortest circuit on a map that makes a tour of specified sites.

Strand 3: Patterns, Algebra, and Functions

Concept 1: Patterns

Identify patterns and apply pattern recognition to reason mathematically.

- PO 1. *Communicate a grade-level appropriate recursive pattern, using symbols or numbers.*
Alternate: Identify the rule for a pattern of symbols or numbers.
- PO 2. Extend a grade-level appropriate recursive pattern.
Alternate: Extend a pattern using symbols or numbers.
- PO 3. Solve grade-level appropriate recursive pattern problems.

Concept 2: Functions and Relationships

Describe and model functions and their relationships.

- PO 1. *Describe the rule used in a simple grade-level appropriate function (e.g., T-chart, input/output model).*

Concept 3: Algebraic Representations

Represent and analyze mathematical situations and structures using algebraic representations.

- PO 1. Evaluate an expression containing two variables by substituting integers for the variable (e.g., $7x + m$, when $x = -4$ and $m = 12$).
Alternate: Evaluate an expression involving addition, subtracting, or multiplication by substituting given integers for the variable.
- PO 2. *Use variables in contextual situations.*
Alternate: Use variables in contextual situations.
- PO 3. Translate a written sentence into a one-step, one-variable algebraic equation.
- PO 4. Translate a sentence written in context into an algebraic equation involving one operation.
- PO 5. Solve one-step equations using inverse operations with positive rational numbers (e.g., $\frac{2}{3}n = 6$).

Concept 4: Analysis of Change

Analyze change in a variable over time and in various contexts.

- PO 1. Analyze change in various linear contextual situations.

Strand 4: Geometry and Measurement

Concept 1: Geometric Properties

Analyze the attributes and properties of 2- and 3- dimensional shapes and develop mathematical arguments about their relationships.

- PO 1. Draw a geometric figure showing specified properties (e.g., Draw an obtuse triangle.).
Alternate: Identify a geometric figure based on specified properties.
- PO 2. Classify 3-dimensional solids by their configuration and properties (e.g., parallelism, perpendicularity and congruency).
Alternate: Classify geometric shapes and figures by specified properties.
- PO 3. Identify the net (2-dimensional representation) that corresponds to a rectangular prism, cone, or cylinder.
- PO 4. Distinguish between length, area, and volume, using 2- and 3-dimensional geometric figures.
- PO 5. Draw polygons with appropriate labels.
- PO 6. Identify the angles created by two lines and a transversal.
- PO 7. Recognize the relationship between central angles and intercepted arcs.
- PO 8. Identify arcs and chords of a circle.
- PO 9. Model the triangle inequality theorem using manipulatives.
- PO 10. Identify corresponding parts of congruent polygons as congruent.

Concept 2: Transformation of Shapes

Apply spatial reasoning to create transformations and use symmetry to analyze mathematical situations.

- PO 1. Identify rotations about a point, using pictorial models.
- PO 2. Recognize simple single rotations, translations or reflections on a coordinate grid.

Concept 3: Coordinate Geometry

Specify and describe spatial relationships using coordinate geometry and other representational systems.

- PO 1. Graph data points in (x, y) form in any quadrant of a coordinate grid.
- PO 2. State the missing coordinate of a given figure in any quadrant of a coordinate grid using geometric properties (e.g., Find the coordinates of the missing vertex of a rectangle when two adjacent sides are drawn.).

Concept 4: Measurement - Units of Measure Geometric Objects

Understand and apply appropriate units of measure, measurement techniques, and formulas to determine measurements.

- PO 1. Identify the appropriate unit of measure for the volume of an object (e.g., cubic inches or cubic cm).
Alternate: Identify an appropriate measure of accuracy for a given contextual situation.
- PO 2. Measure to the appropriate degree of accuracy.
Alternate: Measure to the appropriate degree of accuracy.
- PO 3. Convert a measurement from U.S. customary to metric, and vice versa.
- PO 4. Solve problems involving the circumference of a circle.
- PO 5. Solve problems involving the area of a circle.
Alternate: Solve problems involving the area of a simple polygon.
- PO 6. Solve problems for the areas of parallelograms, triangles, and circles.
- PO 7. Identify polygons having the same perimeter or area.
- PO 8. Compare estimated to actual lengths based on scale drawings or maps.
Alternate: Compare estimated to actual lengths.

Strand 5: Structure and Logic

Concept 1: Algorithms and Algorithmic Thinking

Use reasoning to solve mathematical problems in contextual situations.

PO 1. *Discriminate necessary information from unnecessary information in a given grade-level appropriate word problem.*

PO 2. Analyze algorithms for computing with fractions.

Concept 2: Logic, Reasoning, Arguments, and Mathematical Proof

Evaluate situations, select problem-solving strategies, draw logical conclusions, develop and describe solutions and recognize their applications.

PO 1. Solve a logic problem using multiple variables.

Alternate: Solve a simple logic problem from given information.

MATHEMATICS STANDARD ARTICULATED BY GRADE LEVEL

Grade 8

Instruction for students identified as having a significant cognitive disability should be developed from Arizona's Alternate Academic Standards. Only those performance objectives that have an identified alternate are required. When developing lessons or activities aligned to the grade level alternate standards, teachers should consider individual student abilities and their need for accommodations, cues, manipulatives/objects, augmentative devices, and communication systems. In addition the depth and breadth of the alternate academic standard can be simplified based on the student's current cognitive abilities. Teachers can also develop lessons using performance objectives without alternates for those students who have developed those specific skills.

Strand 1: Number Sense and Operations

Concept 1: Number Sense

Understand and apply numbers, ways of representing numbers, the relationships among numbers and different number systems.

- PO 1. Locate rational numbers on a number line.
Alternate: Locate rational numbers (positive and negative) on a number line.
- PO 2. Identify irrational numbers.
- PO 3. Classify real numbers as rational or irrational.

Concept 2: Numerical Operations

Understand and apply numerical operations and their relationship to one another.

- PO 1. *Select the grade-level appropriate operation to solve word problems.*
Alternate: Select addition, subtraction, multiplication, or division to solve word problems.
- PO 2. *Solve word problems using grade-level appropriate operations and numbers.*
Alternate: Solve word problems using addition, subtraction, multiplication, or division.
- PO 3. Determine the square of an integer.
- PO 4. Determine the square root of an integer.
- PO 5. Identify squaring and finding square roots as inverse operations.
- PO 6. *Apply grade-level appropriate properties to assist in computation.*
- PO 7. Apply the symbols " $\sqrt{\quad}$ " to represent square root, " \pm " to represent roots, and " $\{\}$ " as grouping symbols.
- PO 8. *Use grade-level appropriate mathematical terminology.*
- PO 9. Calculate the missing value in a percentage problem.

PO 10. Convert standard notation to scientific notation, and vice versa.

PO 11. *Simplify numerical expressions using the order of operations with grade- appropriate operations on number sets.*

Concept 3: Estimation

Use estimation strategies reasonably and fluently.

PO 1. *Solve grade-level appropriate problems using estimation.*

Alternate: Solve problems using estimation in a contextual situation.

PO 2. *Use estimation to verify the reasonableness of a calculation (e.g., Is 32 the square root of 64?).*

PO 3. Express answers to the appropriate place or degree of precision (e.g., time, money).

PO 4. *Verify the reasonableness of estimates made from calculator results within a contextual situation.*

Alternate: Estimate and check on a calculator.

Strand 2: Data Analysis, Probability, and Discrete Mathematics

Concept 1: Data Analysis (Statistics)

Understand and apply data collection, organization and representation to analyze and sort data.

- PO 1. *Formulate questions to collect data in contextual situations.*
- PO 2. Construct box-and-whisker plots.
- PO 3. Determine the appropriate type of graphical display for a given data set.
- PO 4. Interpret box-and-whisker plots, circle graphs, and scatter plots.
Alternate: Interpret simple displays of data for bar graphs, tally charts, line graphs, circle graphs, or Venn diagrams.
- PO 5. Answer questions based on box-and-whisker plots, circle graphs, and scatter plots.
- PO 6. Solve problems in contextual situations using the mean, median, mode, and range of a given data set.
- PO 7. Formulate reasonable predictions based on a given set of data.
- PO 8. Compare trends in data related to the same investigation.
- PO 9. Solve contextual problems using scatter plots, box-and-whiskers plots, and double line graphs of continuous data.
Alternate: Solve problems using bar graphs, tally charts, line graphs, circle graphs, or Venn diagrams.
- PO 10. Evaluate the effects of missing or incorrect data on the results of an investigation (e.g., Susie's teacher recorded a 39 instead of a 93 for her last quiz, what will happen to Susie's average?).
- PO 11. Identify a line of best fit for a scatter plot.
- PO 12. Distinguish between causation and correlation.

Concept 2: Probability

Understand and apply the basic concepts of probability.

- PO 1. Determine the probability that a specific event will occur in a 2-stage probability experiment.
- PO 2. Solve contextual situations using probability (e.g., If the probability of Michelle making a free throw is 0.25, what is the probability that she will make three free throws in a row?).
- PO 3. *Predict the outcome of a grade-level appropriate probability experiment.*
Alternate: Predict the outcome of a probability experiment.
- PO 4. *Record the data from performing a grade-level appropriate probability experiment.*
Alternate: Record the data from a probability experiment.
- PO 5. *Compare the outcome of an experiment to predictions made prior to performing the experiment.*
Alternate: Compare the outcome of an experiment to predictions made prior to performing the experiment.

PO 6. Distinguish between independent and dependent events.

PO 7. *Compare the results of two repetitions of the same grade-level appropriate probability experiment.*

Alternate: Compare the results of two repetitions of the same probability experiment.

Concept 3: Discrete Mathematics – Systematic Listing and Counting

Understand and demonstrate the systematic listing and counting of possible outcomes.

PO 1. Determine all possible outcomes involving the combination of two or more sets of objects (e.g., If you roll a six-sided number cube 4 times, how many possible outcomes are possible?).

PO 2. Determine all possible arrangements given a set (e.g., How many ways can you arrange a set of 7 books on a shelf?).

Concept 4: Vertex-Edge Graphs

Understand and apply vertex-edge graphs.

PO 1. Solve contextual problems represented by vertex-edge graphs.

Alternate: Find the shortest circuit on a map that makes a tour of specified sites in contextual situations.

Strand 3: Patterns, Algebra, and Functions

Concept 1: Patterns

Identify patterns and apply pattern recognition to reason mathematically.

PO 1. Communicate a grade-level appropriate iterative or recursive pattern, using symbols or numbers.

Alternate: Identify the rule of a pattern of symbols or numbers.

PO 2. Extend a grade-level appropriate iterative or recursive pattern.

Alternate: Extend a pattern using symbols or numbers.

PO 3. Solve grade-level appropriate iterative or recursive pattern problems.

Concept 2: Functions and Relationships

Describe and model functions and their relationships.

PO 1. Describe the rule used in a simple grade-level appropriate function (e.g., T-chart, input/output model).

PO 2. Distinguish between linear and nonlinear functions, given graphic examples.

PO 3. Determine whether a graph or table is related to a given equation of the form $y=ax^2$ where 'a' is a natural number.

PO 4. Identify independent and dependent variables for a contextual situation.

Concept 3: Algebraic Representations

Represent and analyze mathematical situations and structures using algebraic representations.

PO 1. Evaluate algebraic expressions by substituting rational values for variables [e.g., $2(ab+ac+bc)$, when $a = 2$, $b = 3/5$, and $c = 4$].

Alternate: Evaluate an expression involving addition, subtracting, or multiplication by substituting given integers for the variable.

PO 2. Use variables in contextual situations.

Alternate: Use variables in contextual situations

PO 3. Translate a written sentence or phrase into an algebraic equation or expression, and vice versa (e.g., Three less than twice a number is $2n-3$).

PO 4. Translate a sentence written in context into an algebraic equation involving two operations.

PO 5. Translate a contextual situation into an algebraic inequality (e.g., Joe earns more than \$5.00 an hour; therefore, $x > 5$).

PO 6. Identify an equation or inequality that represents a contextual situation.

PO 7. Solve one-step equations with rational numbers as coefficients or as solutions.

PO 8. Solve one-step equations that model contextual situations.

PO 9. Solve two-step equations with rational coefficients and integer solutions (e.g., $3x + 5 = 11$, $4x - 20 = 8$).

PO 10. Graph an inequality on a number line.

PO 11. Solve a simple algebraic proportion.

PO 12. Solve applied problems using the Pythagorean theorem.

Concept 4: Analysis of Change

Analyze change in a variable over time and in various contexts.

PO 1. Identify the slope of a line as the rate of change (the ratio of rise over run).

Strand 4: Geometry and Measurement

Concept 1: Geometric Properties

Analyze the attributes and properties of 2- and 3- dimensional shapes and develop mathematical arguments about their relationships.

- PO 1. Draw a model that demonstrates basic geometric relationships such as parallelism, perpendicularity, similarity/proportionality, and congruence.
Alternate: Identify a geometric figure based on specified properties.
- PO 2. Draw 3-dimensional figures by applying properties of each (e.g., parallelism, perpendicularity, congruency).
Alternate: Classify geometric figures and shapes by specified properties.
- PO 3. Recognize the 3-dimensional figure represented by a net.
- PO 4. Represent the surface area of rectangular prisms and cylinders as the area of their net.
- PO 5. Draw regular polygons with appropriate labels.
- PO 6. Identify the properties of angles created by a transversal intersecting two parallel lines (e.g., corresponding angles are congruent).
- PO 7. Recognize the relationship between inscribed angles and intercepted arcs.
- PO 8. Identify tangents and secants of a circle.
- PO 9. Determine whether three given lengths can form a triangle.
- PO 10. Identify corresponding angles of similar polygons as congruent and sides as proportional.

Concept 2: Transformation of Shapes

Apply spatial reasoning to create transformations and use symmetry to analyze mathematical situations.

- PO 1. Identify the planar geometric figure that is the result of a given rigid transformation.
- PO 2. Model a simple transformation on a coordinate grid (e.g., Translate right four units and down two units.).

Concept 3: Coordinate Geometry

Specify and describe spatial relationships using coordinate geometry and other representational systems.

- PO 1. Use a table of values to graph a linear equation.
- PO 2. Determine the midpoint given two points on a number line.
Alternate: Determine the midpoint of a line given at least two choices on the line.
- PO 3. Determine the distance between two points on a number line.
Alternate: Determine the distance between two points on a number line.

**Concept 4: Measurement - Units of Measure
- Geometric Objects**

Understand and apply appropriate units of measure, measurement techniques, and formulas to determine measurements.

- PO 1. Solve problems for the area of a trapezoid.
- PO 2. Solve problems involving the volume of rectangular prisms and cylinders.
- PO 3. Calculate the surface area of rectangular prisms or cylinders.
Alternate: Solve problems involving the area of a simple polygon.
- PO 4. Identify rectangular prisms and cylinders having the same volume.
- PO 5. Find the measure of a missing interior angle in a triangle or quadrilateral.
- PO 6. Solve problems using ratios and proportions, given the scale factor.
- PO 7. Calculate the length of a side, given two similar triangles.

Strand 5: Structure and Logic

Concept 1: Algorithms and Algorithmic Thinking

Use reasoning to solve mathematical problems in contextual situations.

PO 1. Describe how to use a proportion to solve a problem in context.

PO 2. Analyze algorithms.

Concept 2: Logic, Reasoning, Arguments, and Mathematical Proof

Evaluate situations, select problem-solving strategies, draw logical conclusions, develop and describe solutions and recognize their applications.

PO 1. *Solve a logic problem given the necessary information.*

Alternate: Solve a simple logic problem from given information.

PO 2. Identify simple valid arguments using *if...then* statements (e.g., All squares are rectangles. If quadrilateral ABCD is a rectangle, is it a square?).

Alternate: Construct simple valid arguments using if...then statements.

PO 3. Model a contextual situation using a flow chart.

PO 4. Verify the Pythagorean theorem using an area dissection argument.

MATHEMATICS STANDARD ARTICULATED BY GRADE LEVEL

High School

Instruction for students identified as having a significant cognitive disability should be developed from Arizona's Alternate Academic Standards. Only those performance objectives that have an identified alternate are required. When developing lessons or activities aligned to the grade level alternate standards, teachers should consider individual student abilities and their need for accommodations, cues, manipulatives/objects, augmentative devices, and communication systems. In addition the depth and breadth of the alternate academic standard can be simplified based on the student's current cognitive abilities. Teachers can also develop lessons using performance objectives without alternates for those students who have developed those specific skills.

Strand 1: Number Sense and Operations

Concept 1: Number Sense	
Understand and apply numbers, ways of representing numbers, the relationships among numbers and different number systems.	
PO 1.	Classify real numbers as members of one or more subsets: natural, whole, integers, rational, or irrational numbers. Alternate: Locate rational numbers (positive and negative) on a number line.
PO 2.	Identify properties of the real number system: commutative, associative, distributive, identity, inverse, and closure. Alternate: Identify commutative property when adding or multiplying.
PO 3.	Distinguish between finite and infinite sets of numbers.

Concept 2: Numerical Operations	
Understand and apply numerical operations and their relationship to one another.	
PO 1.	Select the grade-level appropriate operation to solve word problems. Alternate: Select addition, subtraction, multiplication, or division to solve word problems.
PO 2.	Solve word problems using grade-level appropriate operations and numbers. Alternate: Solve word problems using addition, subtraction, multiplication or division.
PO 3.	Simplify numerical expressions including signed numbers and absolute values.
PO 4.	Apply subscripts to represent ordinal position. Alternate: Identify ordinal numbers.
PO 5.	<i>Use grade level-appropriate mathematical terminology.</i>
PO 6.	Compute using scientific notation.
PO 7.	Simplify numerical expressions using the order of operations.

Concept 3: Estimation

Use estimation strategies reasonably and fluently.

PO 1. *Solve grade-level appropriate problems using estimation.*

Alternate: Solve problems using estimation in a contextual situation.

PO 2. Determine if a solution to a problem is reasonable.

PO 3. Determine rational approximations of irrational numbers.

Strand 2: Data Analysis, Probability, and Discrete Mathematics

Concept 1: Data Analysis (Statistics)

Understand and apply data collection, organization and representation to analyze and sort data.

- PO 1. *Formulate questions to collect data in contextual situations.*
Alternate: Formulate questions to collect data.
- PO 2. Organize collected data into an appropriate graphical representation.
Alternate: Organize data into an appropriate graphical representation.
- PO 3. Display data as lists, tables, matrices, and plots.
- PO 4. Construct equivalent displays of the same data.
Alternate: Construct two different displays of the same data.
- PO 5. Identify graphic misrepresentations and distortions of sets of data.
- PO 6. Identify which of the measures of central tendency is most appropriate in a given situation.
- PO 7. Make reasonable predictions based upon linear patterns in data sets or scatter plots.
- PO 8. Make reasonable predictions for a set of data, based on patterns.
- PO 9. Draw inferences from charts, tables, graphs, plots, or data sets.
Alternate: Draw conclusions from charts, tables, graphs, or data sets.
- PO 10. Apply the concepts of mean, median, mode, range, and quartiles to summarize data sets.
- PO 11. Evaluate the reasonableness of conclusions drawn from data analysis.
- PO 12. Recognize and explain the impact of interpreting data (making inferences or drawing conclusions) from a biased sample.
- PO 13. Draw a line of best fit for a scatter plot.
- PO 14. Determine whether displayed data has positive, negative, or no correlation.
- PO 15. Identify a normal distribution.
- PO 16. Identify differences between sampling and census.
- PO 17. Identify differences between biased and unbiased samples.

Concept 2: Probability

Understand and apply the basic concepts of probability.

- PO 1. Find the probability that a specific event will occur, with or without replacement.
- PO 2. Determine simple probabilities related to geometric figures.
- PO 3. *Predict the outcome of a grade-level appropriate probability experiment.*
Alternate: Predict an outcome of a probability experiment.
- PO 4. *Record the data from performing a grade-level appropriate probability experiment.*
Alternate: Record the data from a probability experiment.

- PO 5. *Compare the outcome of an experiment to predictions made prior to performing the experiment.*
Alternate: Compare the outcome of an experiment to predictions made prior to performing the experiment.
- PO 6. *Distinguish between independent and dependent events.*
- PO 7. *Compare the results of two repetitions of the same grade-level appropriate probability experiment.*
Alternate: Compare the results of two repetitions of the same appropriate probability experiment.

Concept 3: Discrete Mathematics – Systematic Listing and Counting

Understand and demonstrate the systematic listing and counting of possible outcomes.

- PO 1. Determine the number of possible outcomes for a contextual event using a chart, a tree diagram, or the counting principle.
- PO 2. Determine when to use combinations versus permutations in counting objects.
- PO 3. Use combinations or permutations to solve contextual problems.

Concept 4: Vertex-Edge Graphs

Understand and apply vertex-edge graphs.

(Grades K-8)

Strand 3: Patterns, Algebra, and Functions

Concept 1: Patterns

Identify patterns and apply pattern recognition to reason mathematically.

PO 1. *Communicate a grade-level appropriate iterative or recursive pattern, using symbols or numbers.*

Alternate: Identify the rule of a pattern.

PO 2. *Find the n^{th} term of an iterative or recursive pattern.

Alternate: Extend a pattern.

PO 3. Evaluate problems using basic recursion formulas.

Concept 2: Functions and Relationships

Describe and model functions and their relationships.

PO 1. Determine if a relationship is a function, given a graph, table, or set of ordered pairs.

PO 2. Describe a contextual situation that is depicted by a given graph.

PO 3. Identify a graph that models a given real-world situation.

Alternate: Identify a graph that models a given real-world situation.

PO 4. Sketch a graph that models a given contextual situation.

PO 5. Determine domain and range for a function.

PO 6. Determine the solution to a contextual maximum/minimum problem, given the graphical representation.

PO 7. Express the relationship between two variables using tables/matrices, equations, or graphs.

PO 8. Interpret the relationship between data suggested by tables/matrices, equations, or graphs.

PO 9. Determine from two linear equations whether the lines are parallel, perpendicular, coincident, or intersecting but not perpendicular.

Concept 3: Algebraic Representations

Represent and analyze mathematical situations and structures using algebraic representations.

PO 1. Evaluate algebraic expressions, including absolute value and square roots.

Alternate: Evaluate an expression involving addition, subtraction, or multiplication by substituting given integers for the variable.

PO 2. Simplify algebraic expressions.

PO 3. Multiply and divide monomial expressions with integral exponents.

PO 4. Translate a written expression or sentence into a mathematical expression or sentence.

Alternate: Translate a written expression or sentence into a mathematical expression or equation.

- PO 5. Translate a sentence written in context into an algebraic equation involving multiple operations.
- PO 6. Write a linear equation for a table of values.
- PO 7. Write a linear algebraic sentence that represents a data set that models a contextual situation.
- PO 8. Solve linear (first degree) equations in one variable (may include absolute value).
- PO 9. Solve linear inequalities in one variable.
- PO 10. Write an equation of the line given: two points on the line, the slope and a point on the line, or the graph of the line.
- PO 11. Solve an algebraic proportion.
- PO 12. Solve systems of linear equations in two variables (integral coefficients and rational solutions).
- PO 13. Add, subtract, and perform scalar multiplication with matrices.
- PO 14. Calculate powers and roots of real numbers, both rational and irrational, using technology when appropriate.
- PO 15. Simplify square roots and cube roots with monomial radicands (including those with variables) that are perfect squares or perfect cubes.
- PO 16. Solve square root radical equations involving only one radical.
- PO 17. Solve quadratic equations.
- PO 18. Identify the sine, cosine, and tangent ratios of the acute angles of a right triangle.

Concept 4: Analysis of Change

Analyze change in a variable over time and in various contexts.

- PO 1. Determine slope, x-, and y-intercepts of a linear equation.
- PO 2. Solve formulas for specified variables.

Strand 4: Geometry and Measurement

Concept 1: Geometric Properties

Analyze the attributes and properties of 2- and 3-dimensional shapes and develop mathematical arguments about their relationships.

- PO 1. Identify the attributes of special triangles (isosceles, equilateral, right).
- PO 2. Identify the hierarchy of quadrilaterals.
- PO 3. Make a net to represent a 3-dimensional object.
- PO 4. Make a 3-dimensional model from a net.
Alternate: Make a 3-dimensional model (pyramid, cube, cone, and cylinder).
- PO 5. Draw 2-dimensional and 3-dimensional figures with appropriate labels.
Alternate: Identify 2-dimensional and 3-dimensional figures.
- PO 6. Solve problems related to complementary, supplementary, or congruent angle concepts.
- PO 7. Solve problems by applying the relationship between circles, angles, and intercepted arcs.
- PO 8. Solve problems by applying the relationship between radii, diameters, chords, tangents, or secants.
- PO 9. Solve problems using the triangle inequality property.
- PO 10. Solve problems using special case right triangles.
- PO 11. Determine when triangles are congruent by applying SSS, ASA, AAS, or SAS.
- PO 12. Determine when triangles are similar by applying SAS, SSS, or AA similarity postulates.
- PO 13. Construct a triangle congruent to a given triangle.
- PO 14. Solve contextual situations using angle and side length relationships.

Concept 2: Transformation of Shapes

Apply spatial reasoning to create transformations and use symmetry to analyze mathematical situations.

- PO 1. Sketch the planar figure that is the result of two or more transformations.
- PO 2. Identify the properties of the planar figure that is the result of two or more transformations.
Alternate: Identify slide, rotation, and reflection.
- PO 3. Determine the new coordinates of a point when a single transformation is performed on a planar geometric figure.
- PO 4. Determine whether a given pair of figures on a coordinate plane represents a translation, reflection, rotation, or dilation.
- PO 5. Classify transformations based on whether they produce congruent or similar figures.
- PO 6. Determine the effects of a single transformation on linear or area measurements of a planar geometric figure.

Concept 3: Coordinate Geometry

Specify and describe spatial relationships using coordinate geometry and other representational systems.

- PO 1. Graph a quadratic equation with lead coefficient equal to one.
- PO 2. Graph a linear equation in two variables.
- PO 3. Graph a linear inequality in two variables.
- PO 4. Determine the solution to a system of equations in two variables from a given graph.
- PO 5. Determine the midpoint between two points in a coordinate system.
Alternate: Determine the midpoint of a line given at least two choices on the line.
- PO 6. Determine changes in the graph of a linear function when constants and coefficients in its equation are varied.
- PO 7. Determine the distance between two points in the coordinate system.

Concept 4: Measurement - Units of Measure - Geometric Objects

Understand and apply appropriate units of measure, measurement techniques, and formulas to determine measurements.

- PO 1. Calculate the area of geometric shapes composed of two or more geometric figures.
Alternate: Identify the area of geometric shapes.
- PO 2. Calculate the volumes of 3-dimensional geometric figures.
- PO 3. Calculate the surface areas of 3-dimensional geometric figures.
Alternate: Identify the surface area of 3-dimensional geometric figures.
- PO 4. Compare perimeter, area, or volume of figures when dimensions are changed.
Alternate: Identify perimeter and area on a variety of figures.
- PO 5. Find the length of a circular arc.
- PO 6. Find the area of a sector of a circle.
- PO 7. Solve for missing measures in a pyramid (i.e., slant height, height).
- PO 8. Find the sum of the interior and exterior angles of a polygon.
- PO 9. Solve scale factor problems using ratios and proportions.
- PO 10. Solve applied problems using similar triangles.

Strand 5: Structure and Logic

Concept 1: Algorithms and Algorithmic Thinking

Use reasoning to solve mathematical problems in contextual situations.

- PO 1. Determine whether a given procedure for simplifying an expression is valid.
- PO 2. Determine whether a given procedure for solving an equation is valid.
Alternate: Determine whether a solution to a problem is valid.
- PO 3. Determine whether a given procedure for solving a linear inequality is valid.
- PO 4. Select an algorithm that explains a particular mathematical process.
- PO 5. Determine the purpose of a simple mathematical algorithm.
- PO 6. Determine whether given simple mathematical algorithms are equivalent.

Concept 2: Logic, Reasoning, Arguments, and Mathematical Proof

Evaluate situations, select problem-solving strategies, draw logical conclusions, develop and describe solutions and recognize their applications.

- PO 1. Draw a simple valid conclusion from a given *if...then* statement and a minor premise.
Alternate: Construct simple valid arguments using *if...then* statements.
- PO 2. List related *if... then* statements in logical order.
- PO 3. Write an appropriate conjecture given a certain set of circumstances.
- PO 4. Analyze assertions related to a contextual situation by using principles of logic.
- PO 5. Identify a valid conjecture using inductive reasoning.
- PO 6. Distinguish valid arguments from invalid arguments.
- PO 7. Create inductive and deductive arguments concerning geometric ideas and relationships, such as congruence, similarity, and the Pythagorean relationship.
- PO 8. Critique inductive and deductive arguments concerning geometric ideas and relationships, such as congruence, similarity, and the Pythagorean relationship.
- PO 9. Identify a counterexample for a given conjecture.
- PO 10. Construct a counterexample to show that a given conjecture is false.
- PO 11. State the inverse, converse, or contrapositive of a given statement.
- PO 12. Determine if the inverse, converse, or contrapositive of a given statement is true or false.
- PO 13. Construct a simple formal or informal deductive proof.
- PO 14. Verify characteristics of a given geometric figure using coordinate formulas such as distance, mid-point, and slope to confirm parallelism, perpendicularity, and congruency.
Alternate: Verify characteristics of geometric figures.